

Intrinsic tension in the supernova sector of the local Hubble constant measurement and its implications

CosmoVerse@Lisbon

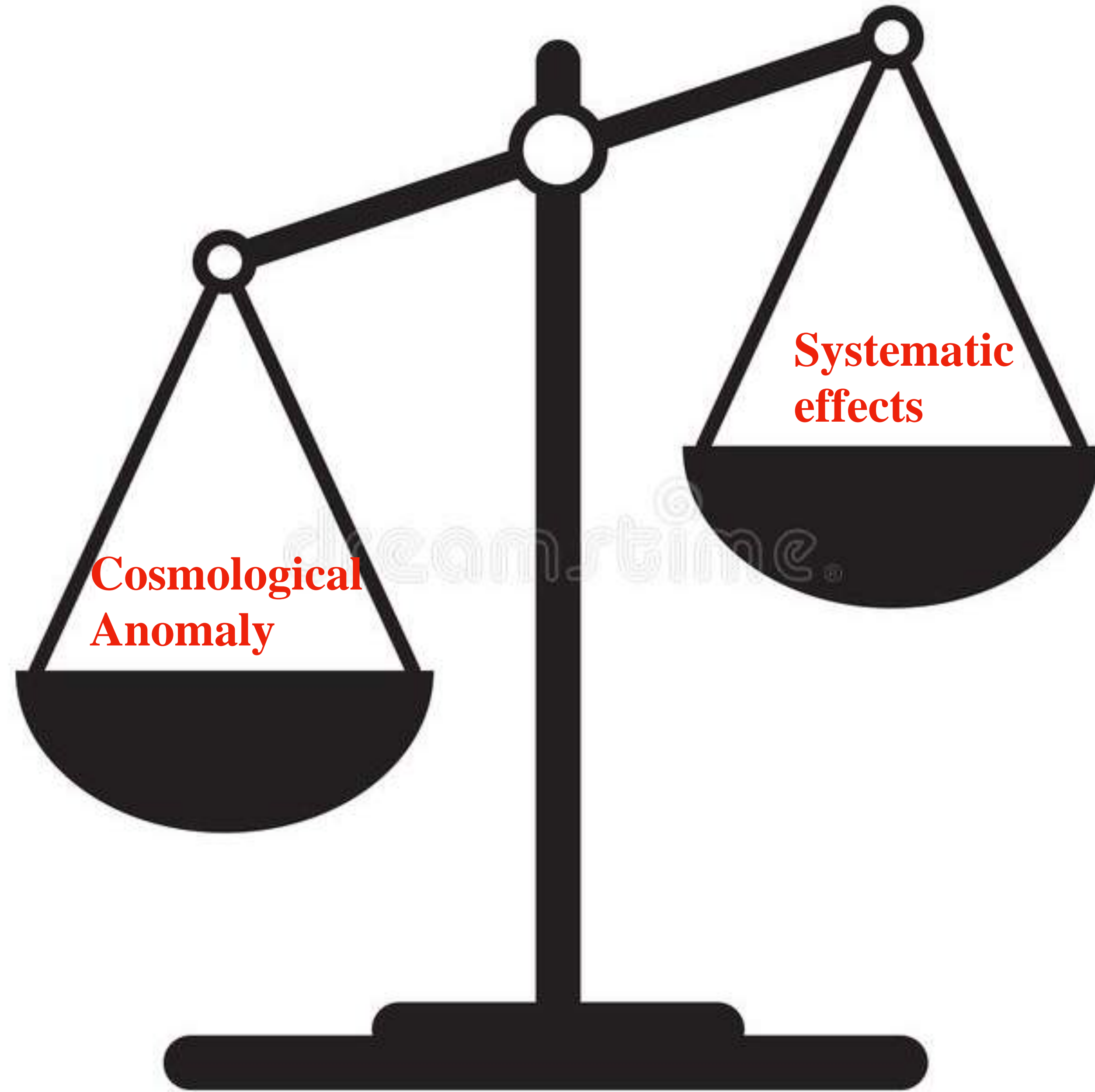
**Radosław (Radek) Wojtak
(DARK, University of Copenhagen)**

Lisbon, 30.05.2023

The H_0 tension: 8% rel. difference, 5σ significance

$$\text{SHOES: } H_0 = 73.04 \pm 1.04 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

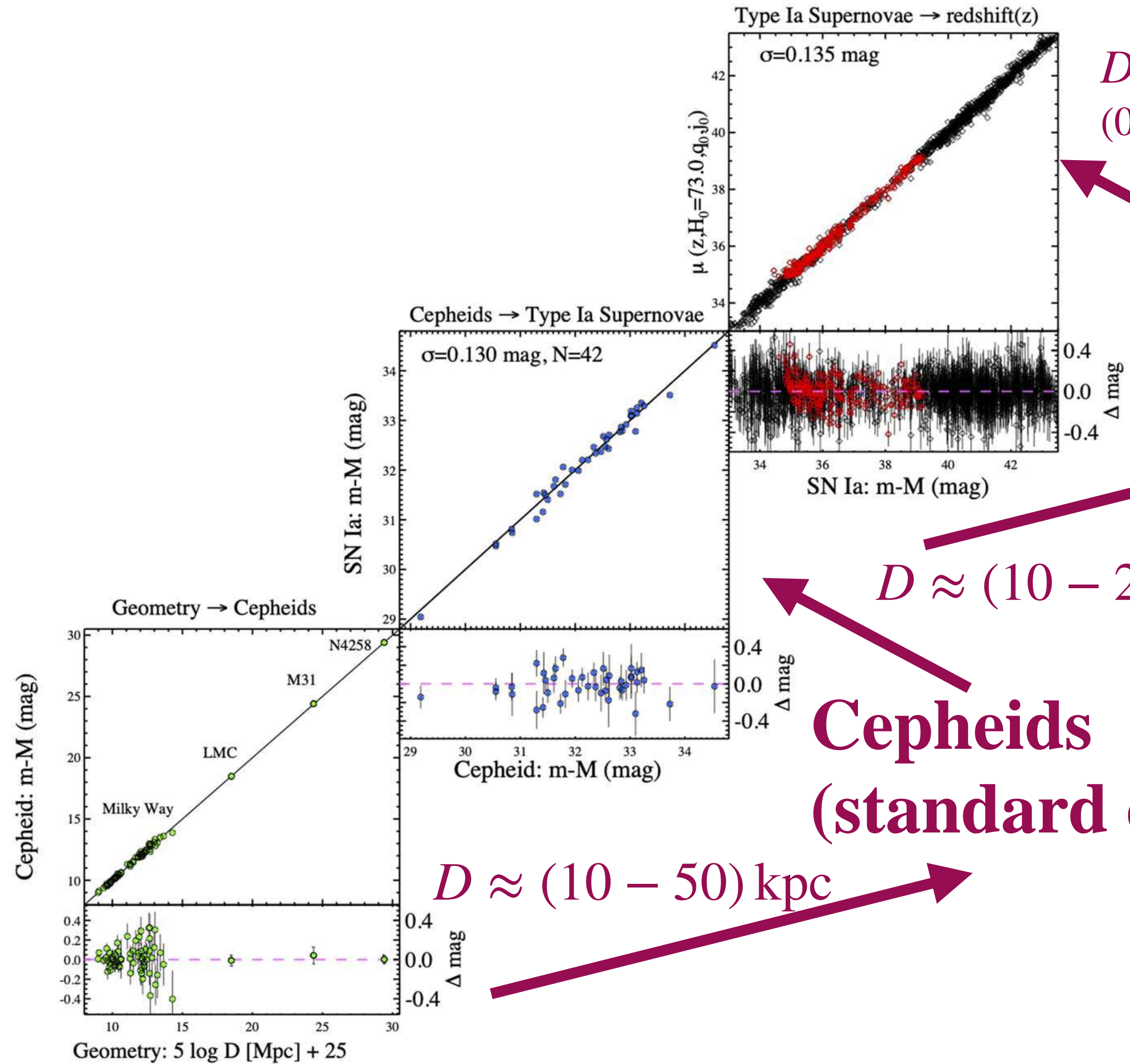
$$\text{Planck(+flat } \Lambda\text{CDM): } H_0 = 67.4 \pm 0.5 \text{ km s}^{-1} \text{ Mpc}^{-1}$$



**Cosmological
Anomaly**

**Systematic
effects**

Direct/local H_0 : distance ladder



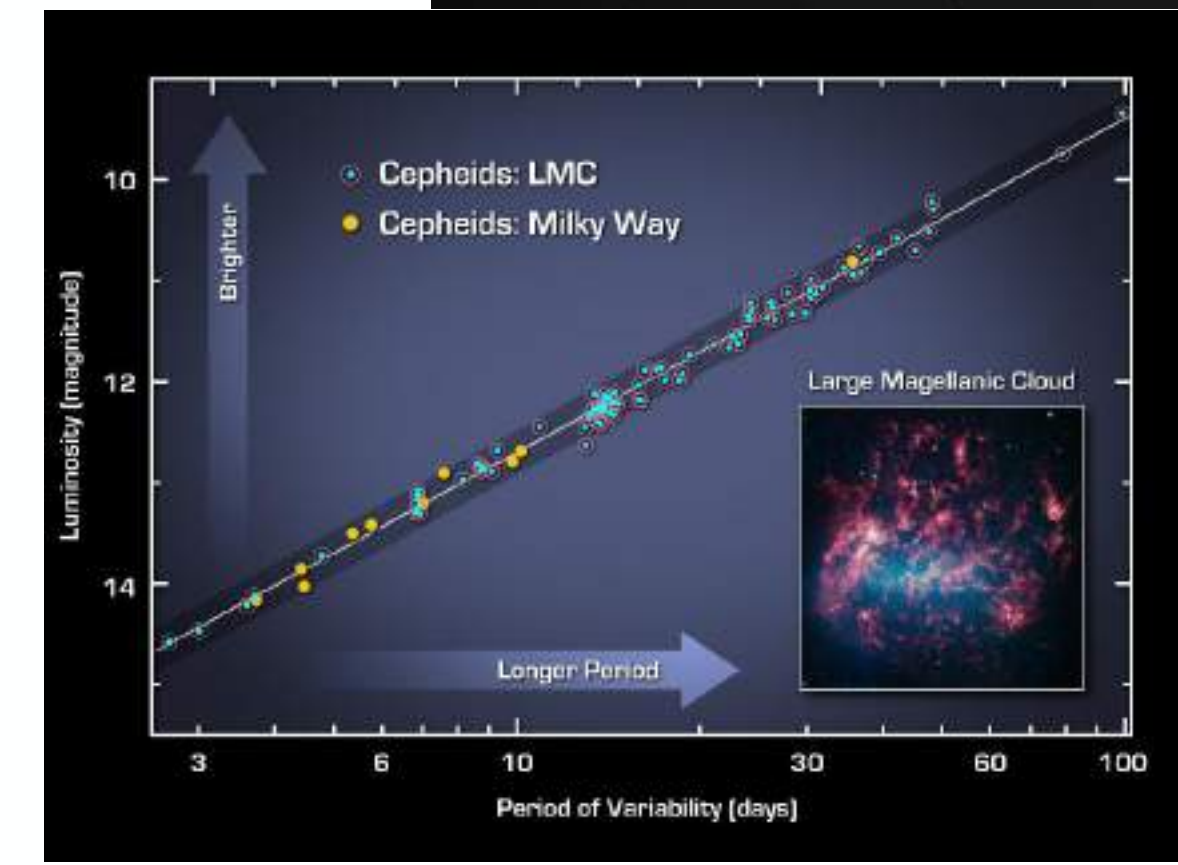
$D \approx (100 - 500) \text{ Mpc}$
 $(0.023 < z < 0.13)$

**Type Ia supernovae
 (Standardisable candles)**

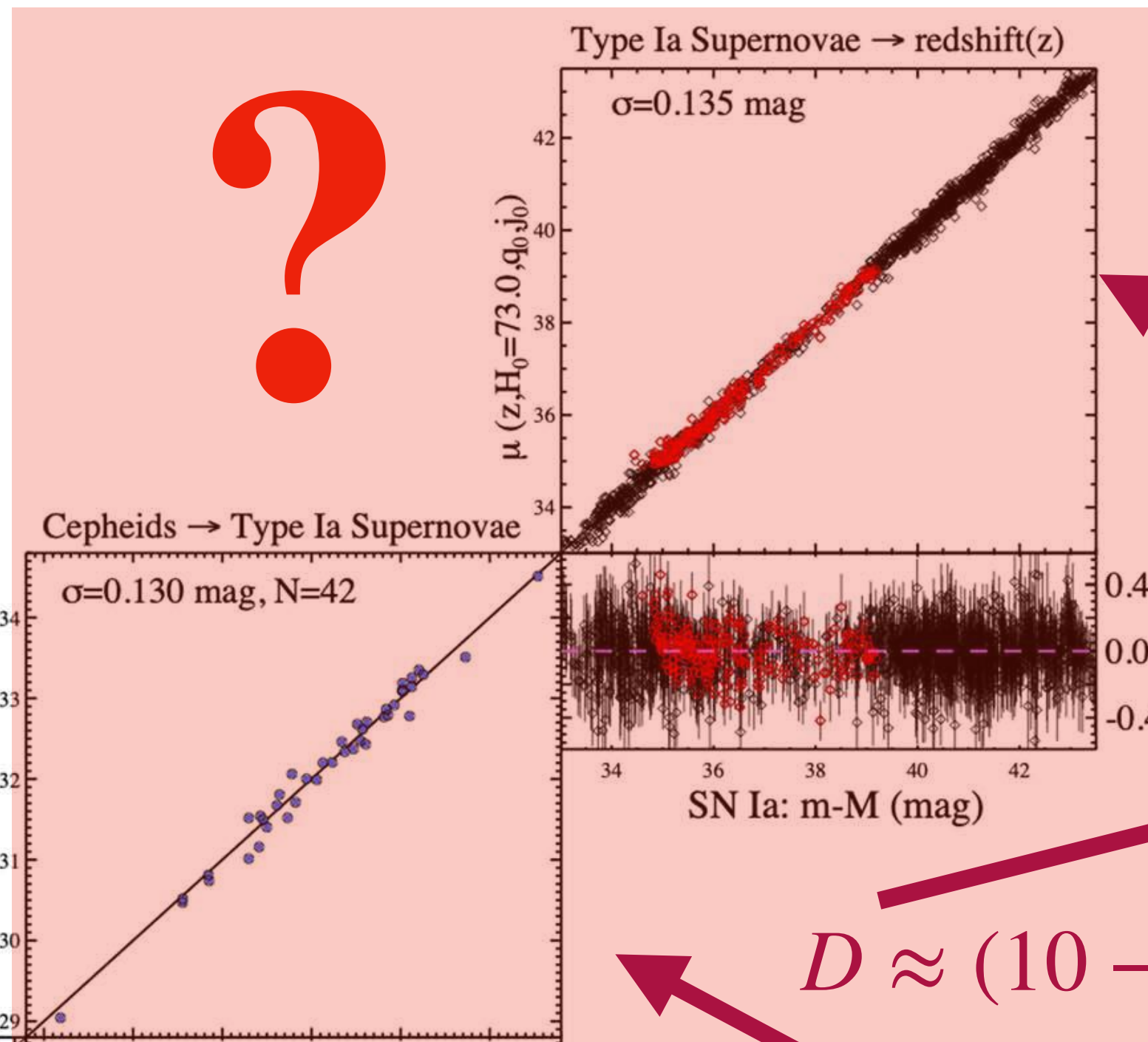
$D \approx (10 - 20) \text{ Mpc}$

**Cepheids
 (standard candles)**

$D \approx (10 - 50) \text{ kpc}$

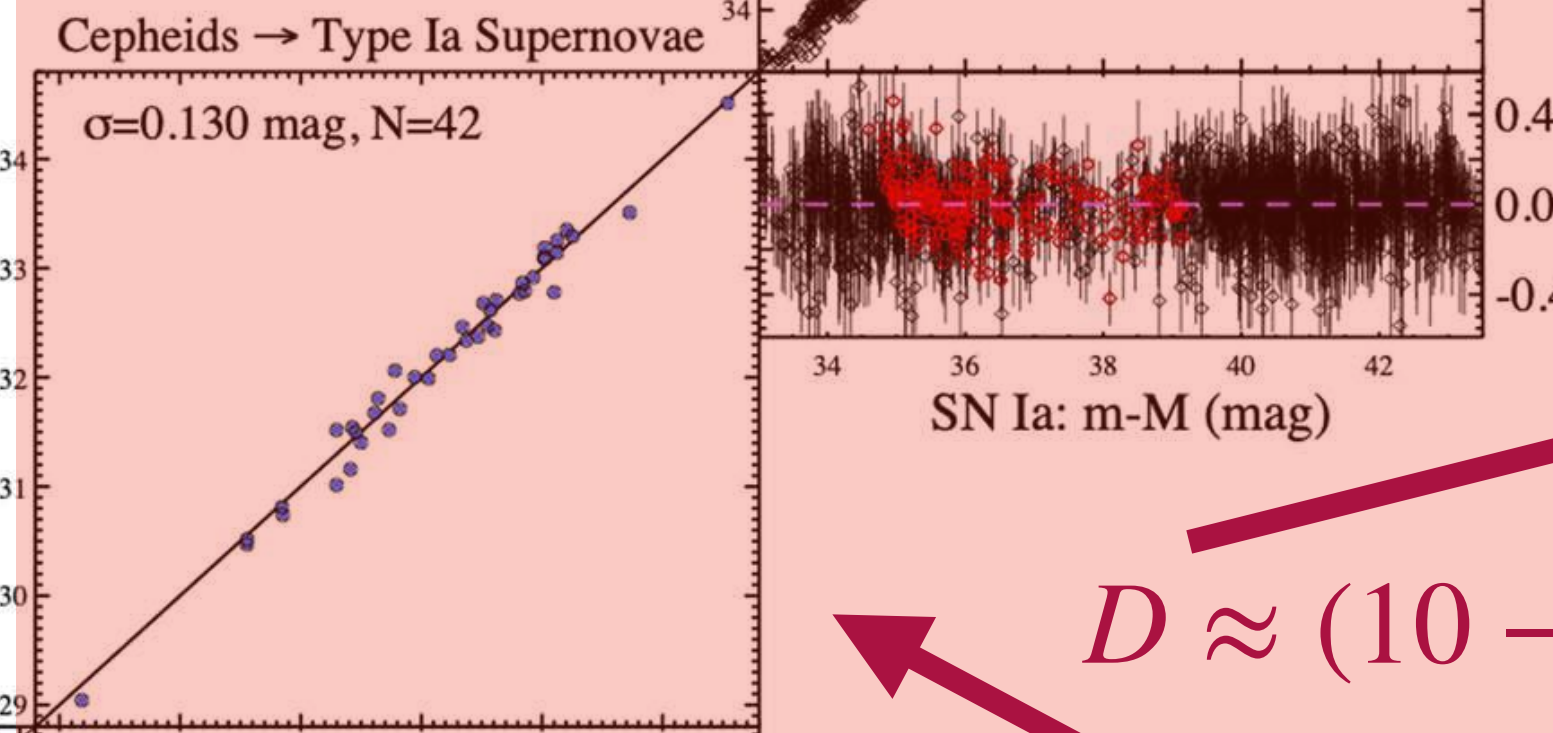


Direct/local H_0 : distance ladder



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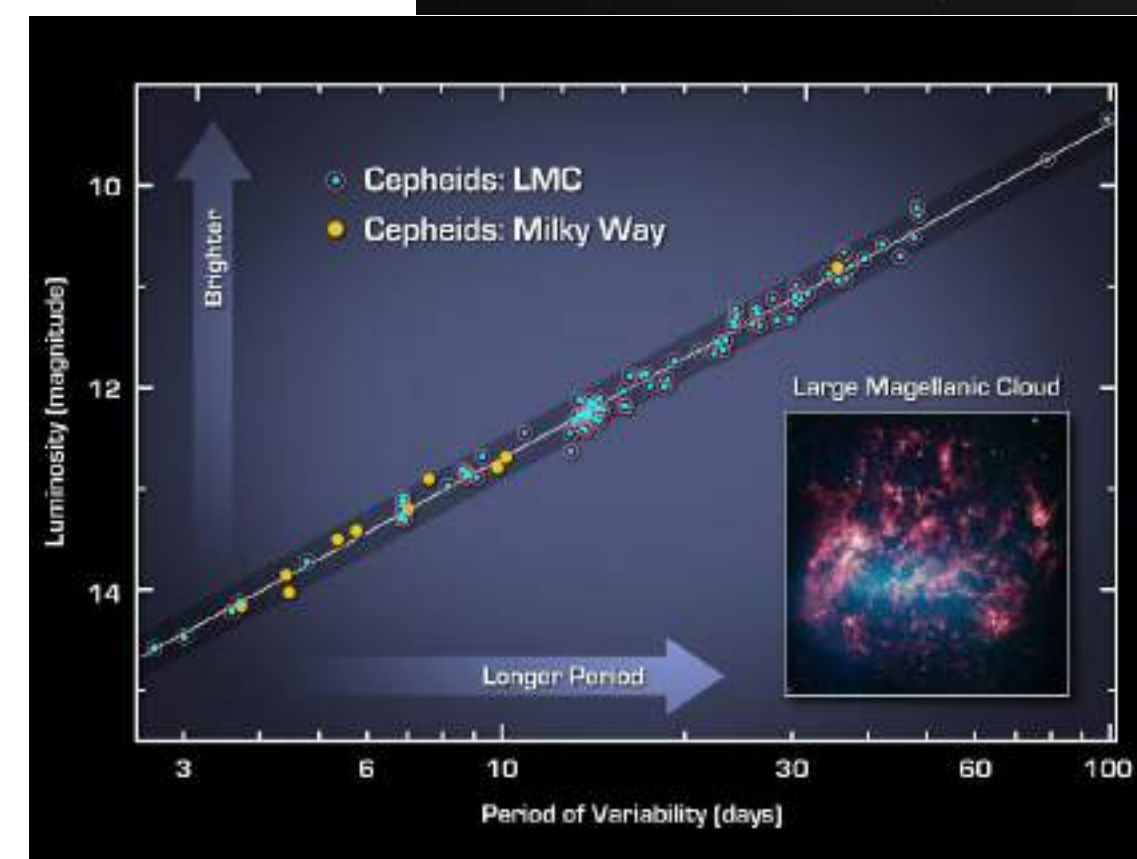
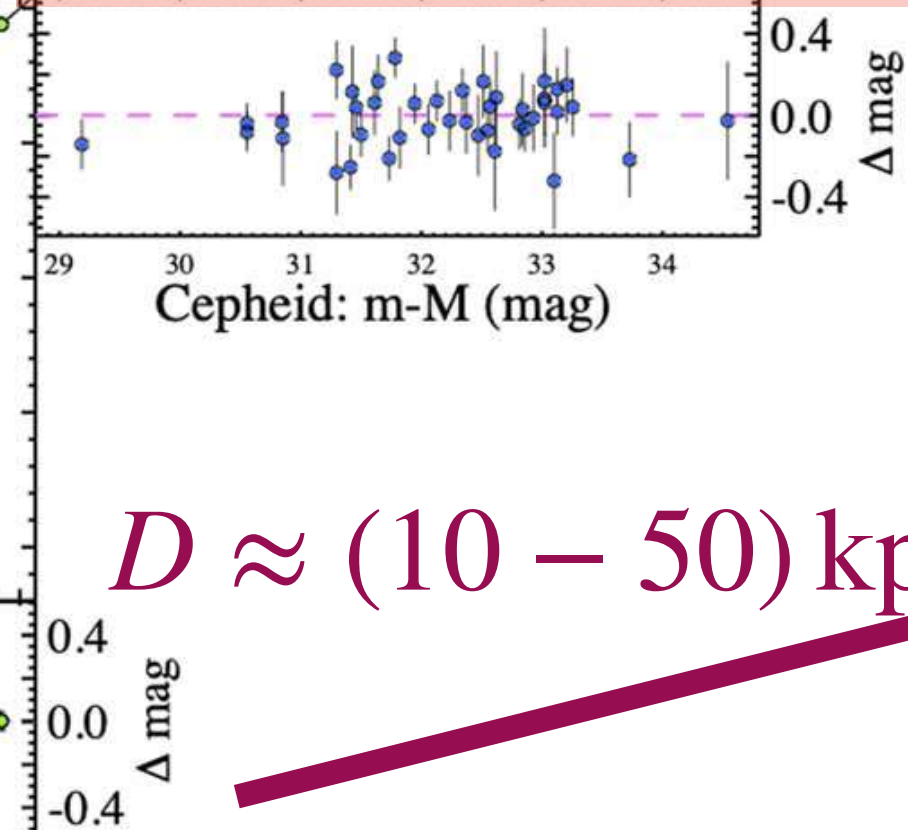
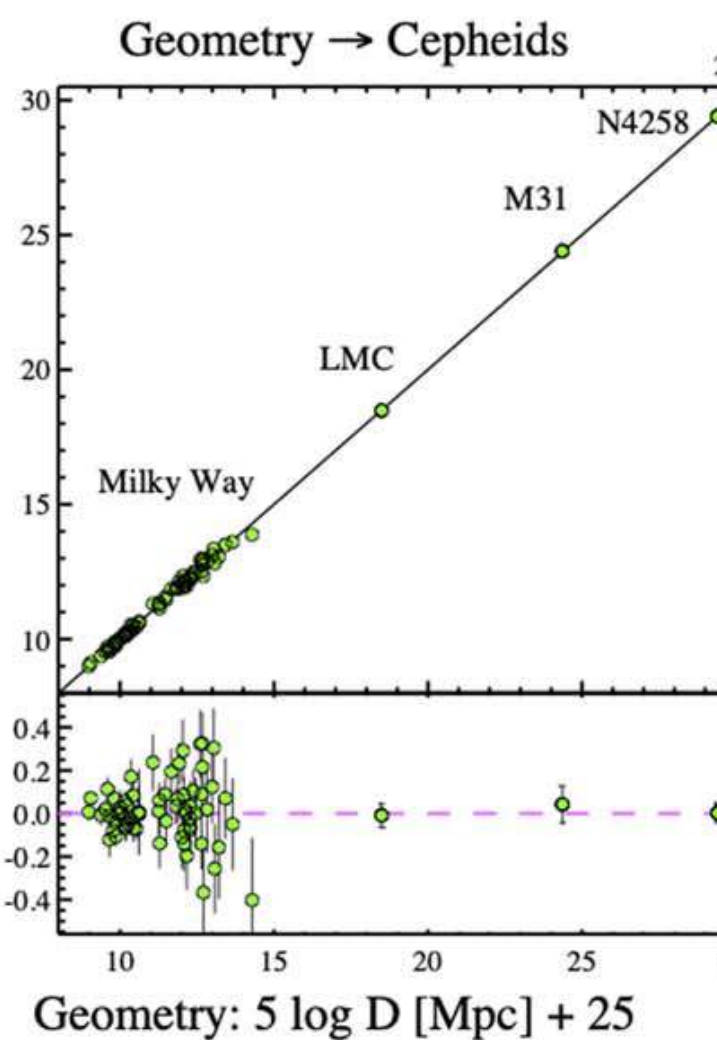
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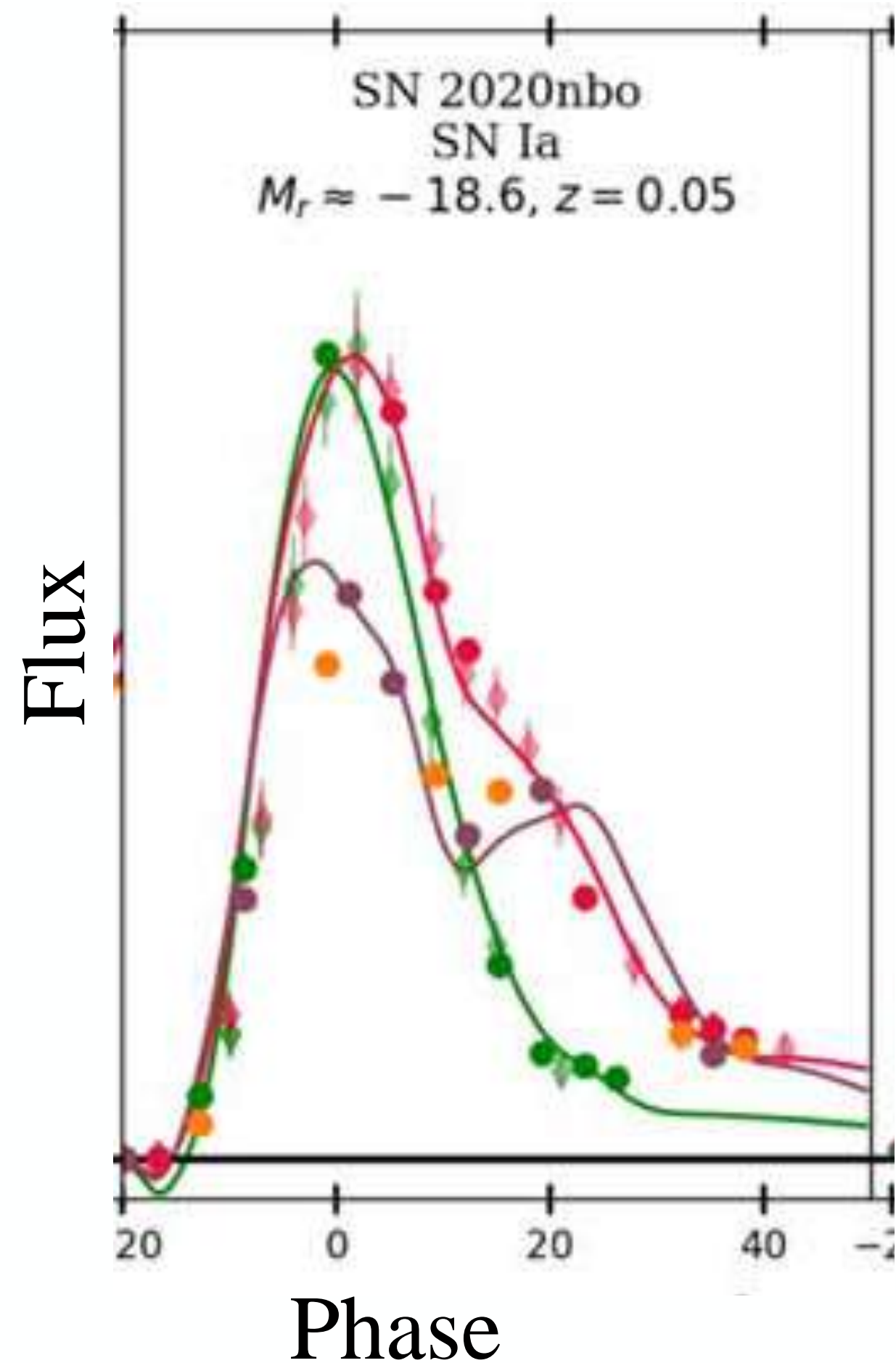
**Cepheids
 (standard candles)**

$D \approx (10 - 50) \text{ kpc}$



Type Ia SN: light curve parameters

Light curves



Empirical models
Based on observed SEDs(t)

Light Curve
Fitting

Light curve parameters:

Peak mag (B band): m_B

Shape parameter (width/rate decline): x_1

Observed colour (B-V): c

Type Ia SN: standardisation

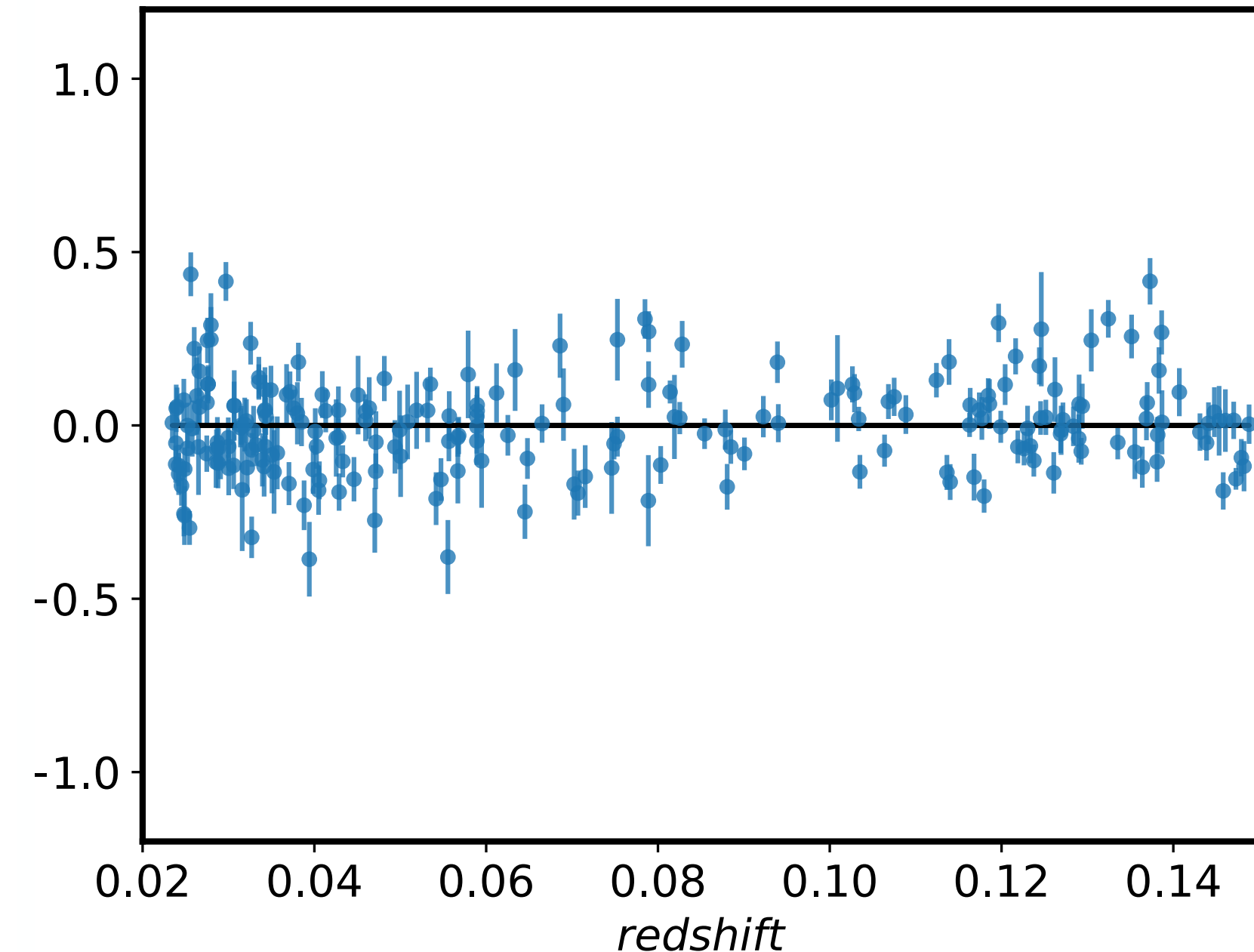
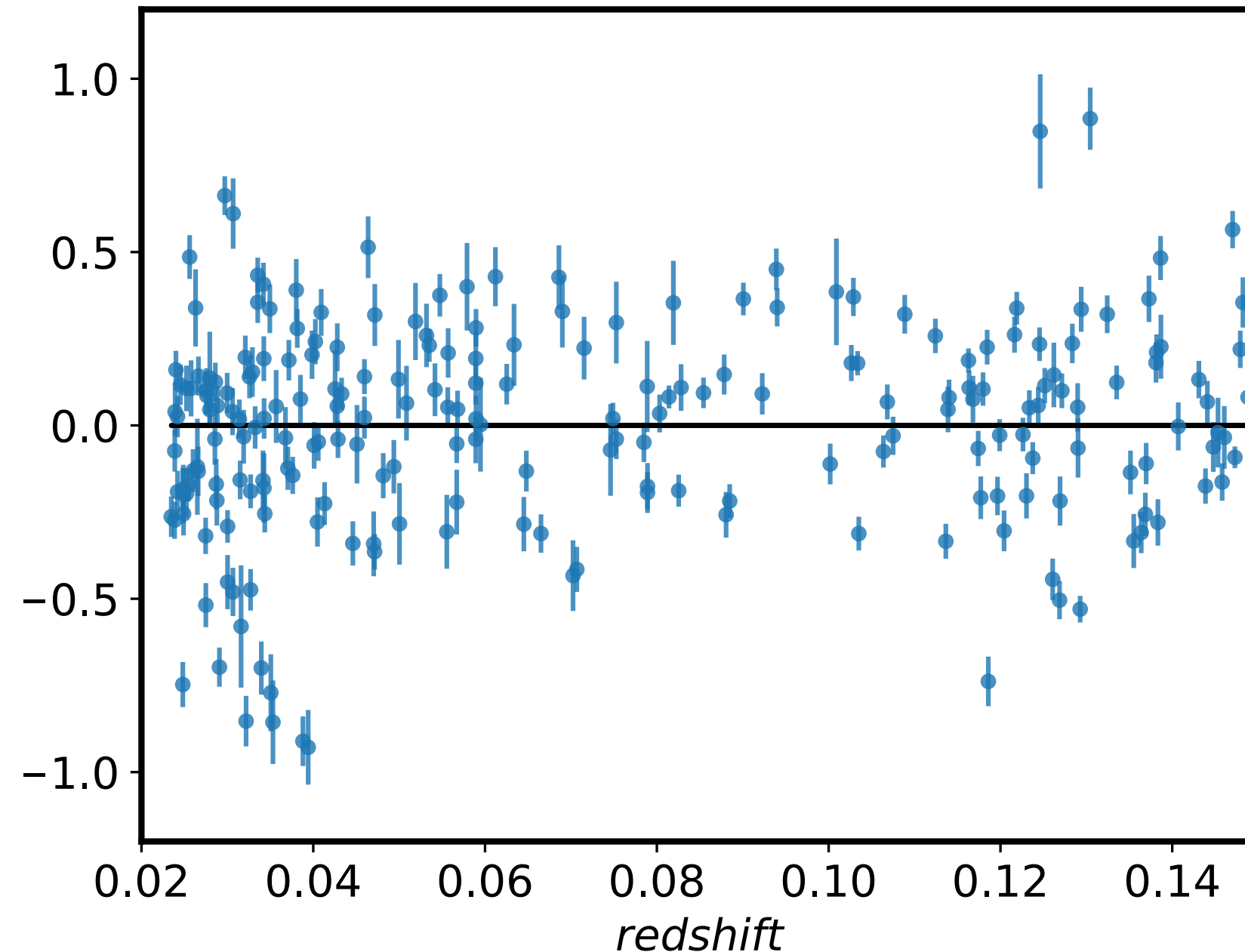
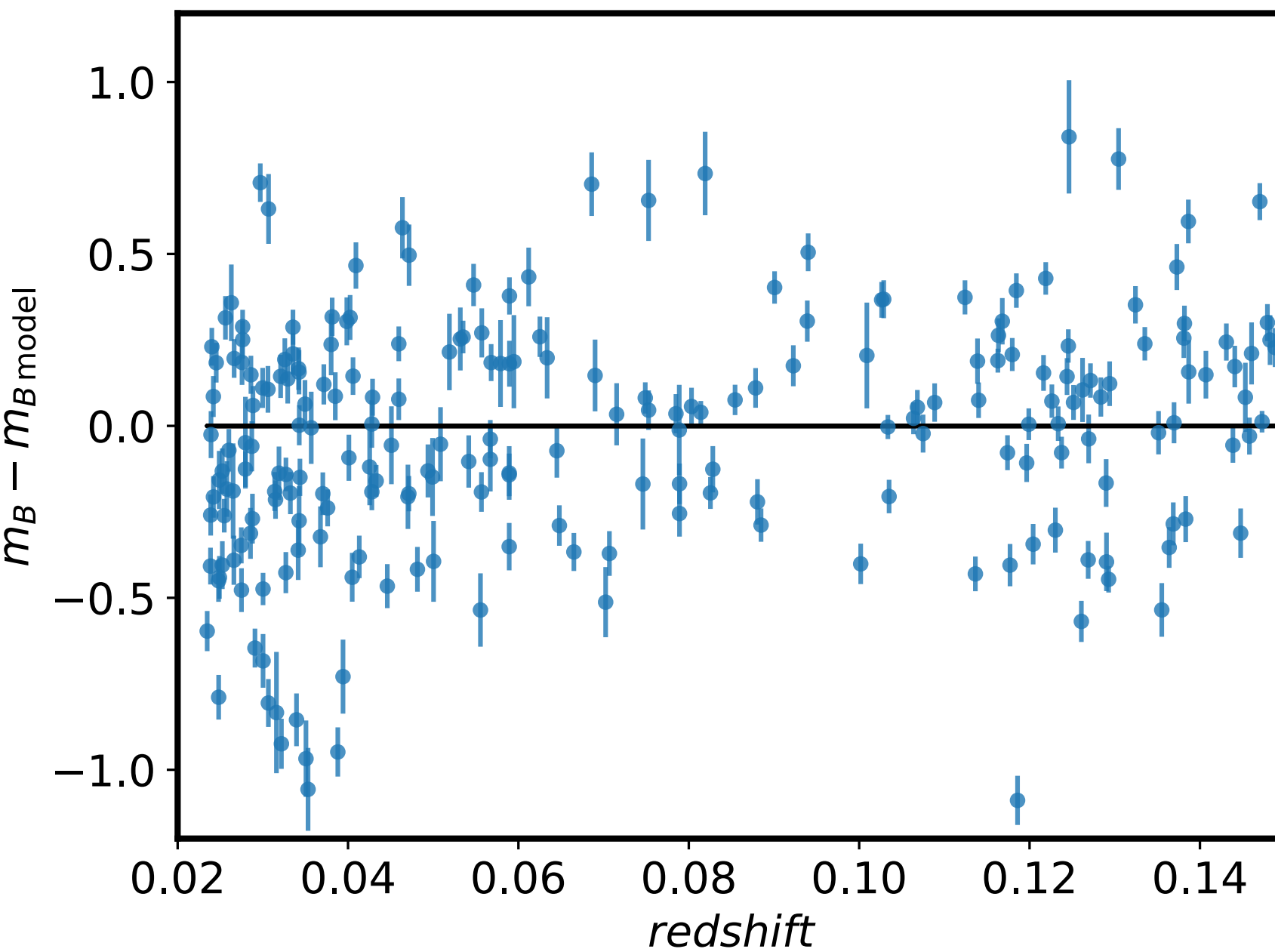
$$m_{\text{model}} = M_{\text{B}} + \mu(z)$$

$$m_{\text{model}} = M_{\text{B}} + \mu(z) + \alpha x_1$$

$$m_{\text{model}} = M_{\text{B}} + \mu(z) + \alpha x_1 + \beta c$$

Phillips relation (Phillips 1995)

Tripp calibration (Tripp 1998)



$$\sigma_{\text{int}} \approx 0.32 \text{ mag}$$

$$\sigma_{\text{int}} \approx 0.27 \text{ mag}$$

Irreducible intrinsic scatter:

$$\sigma_{\text{int}} = 0.12 \text{ mag}$$

Type Ia SN: “standard” standardisation

Fitting strategy: cosmology + Tripp calibration + σ_{int}

$$m_{\text{model}} = M_{\text{B}} + \mu(z) + \alpha x_1 + \beta c$$

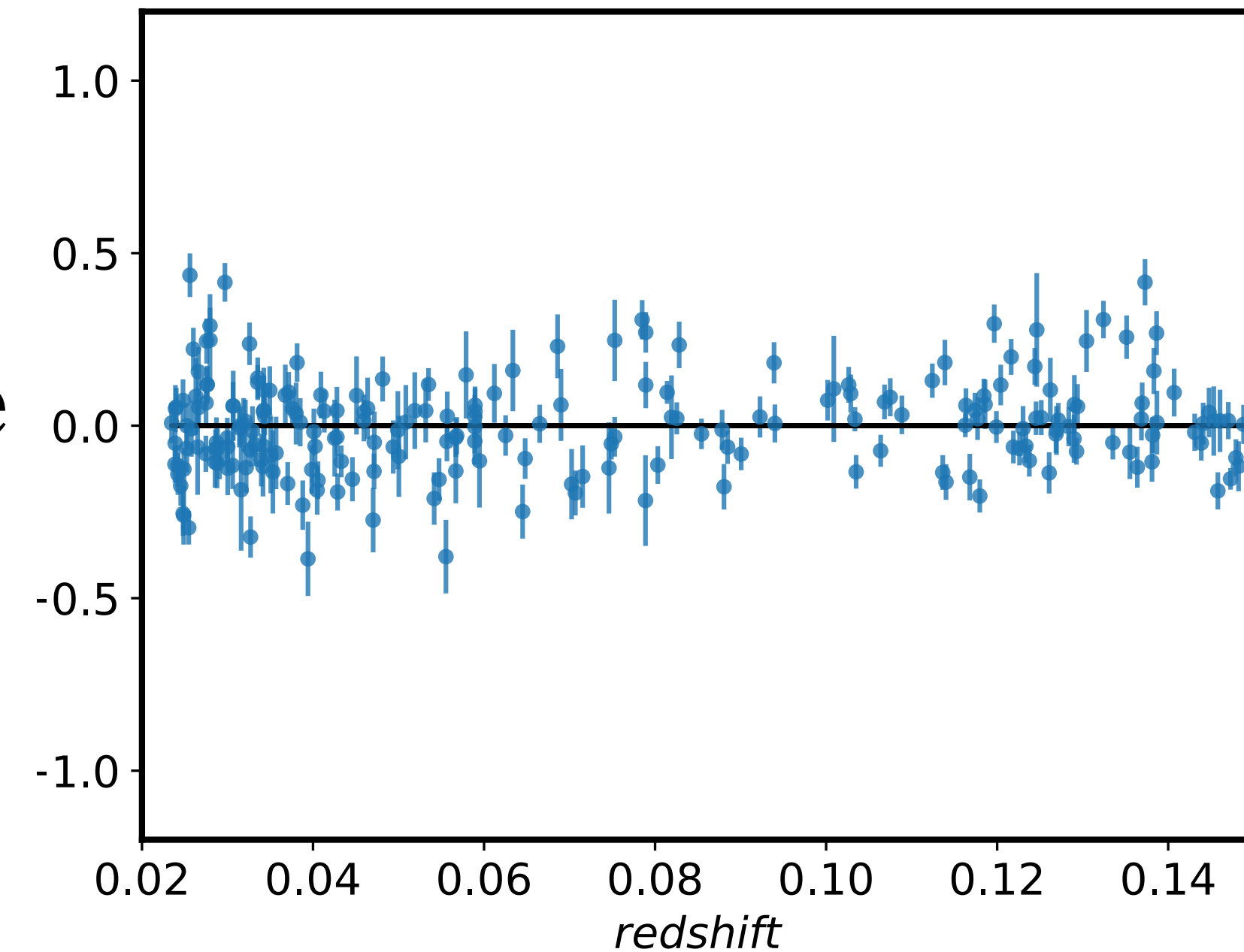
Tripp calibration (Tripp 1998)

(Implicit) assumptions:

- Tripp calibration is universal across redshift and SN samples (calibration vs Hubble flow)
- Distribution of latent variable(s) behind intrinsic scatter is universal across redshift and SN samples: we can effectively decrease error in distance as $\sigma_{\text{int}}/N^{1/2}$

Unresolved problems:

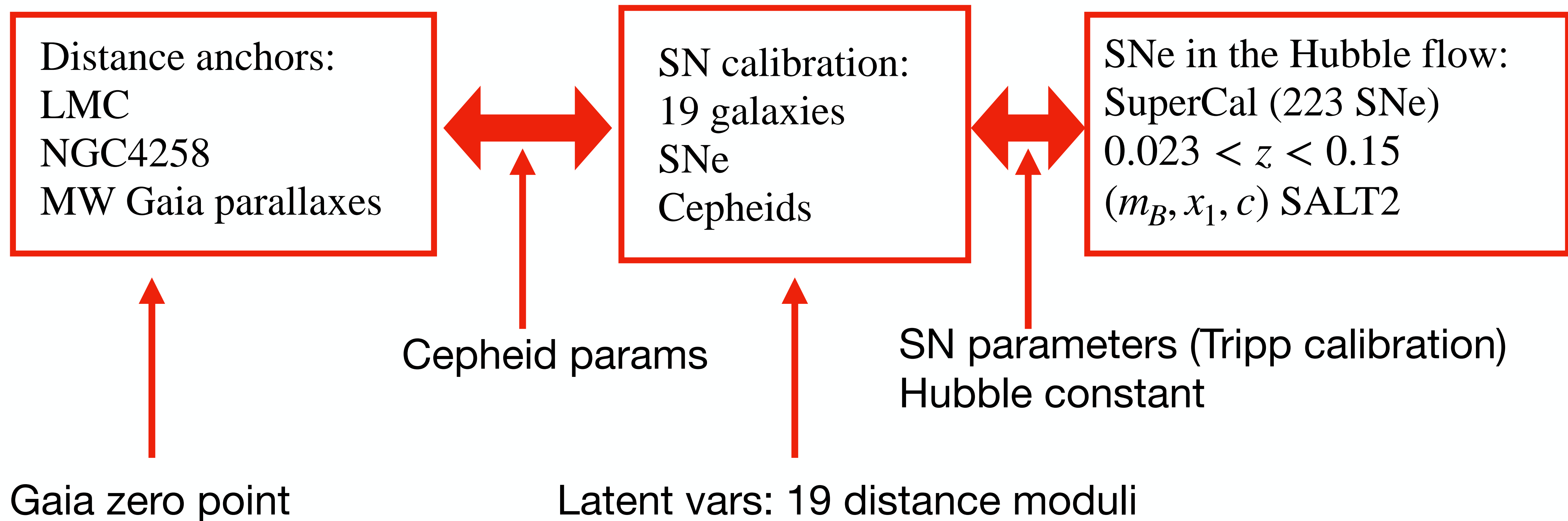
- Physical origin of intrinsic scatter
- Physical origin of the colour correction: extinction in SN host galaxy vs intrinsic colour
- The role of basic physical properties, e.g. two progenitor channels



Irreducible intrinsic scatter:

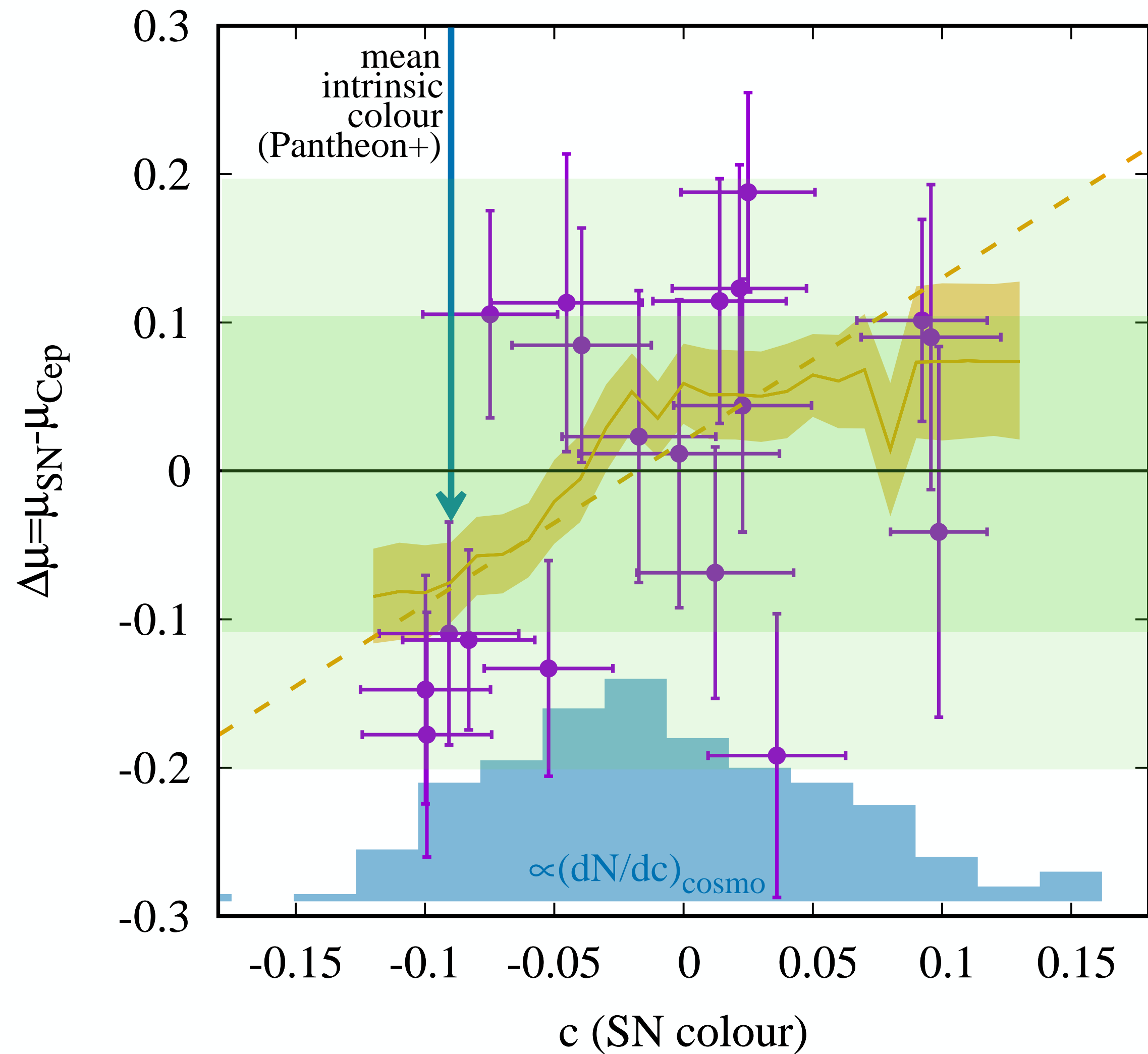
$$\sigma_{\text{int}} = 0.12 \text{ mag}$$

(Pre 2022) SHOES data and global likelihood



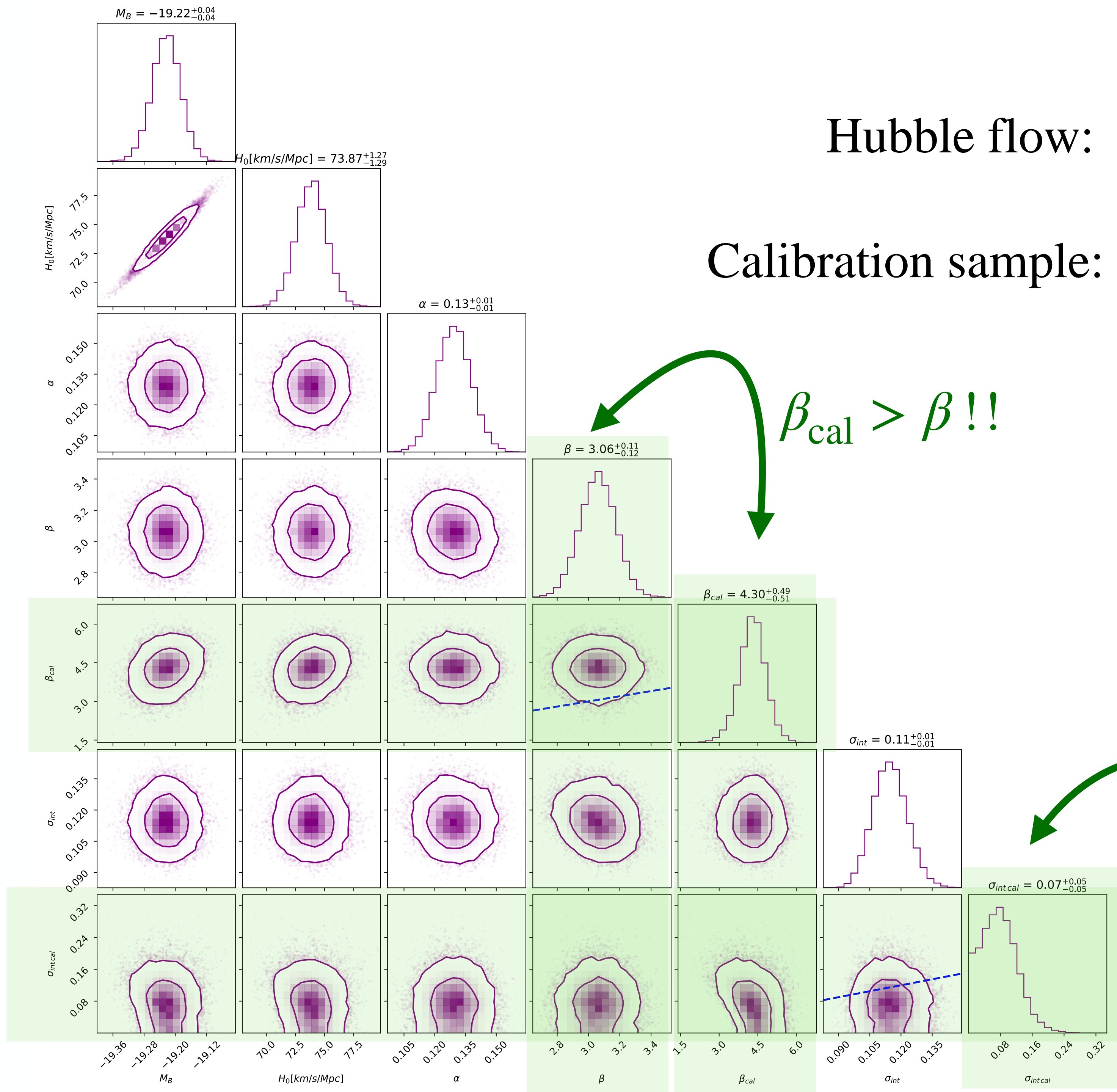
$$L \propto L_{\text{LMC}} \times L_{\text{MW}} \times L_{\text{cal}} \times L_{4258} \times L_{\text{LMC dist}} \times L_{\text{SN cal}} \times L_{\text{SN}}$$

Anomaly in the calibration sample



1 x intrinsic scatter in the Hubble flow

2 x intrinsic scatter in the Hubble flow



Hubble flow: $m_B = M_B - \alpha x_1 + \beta c$

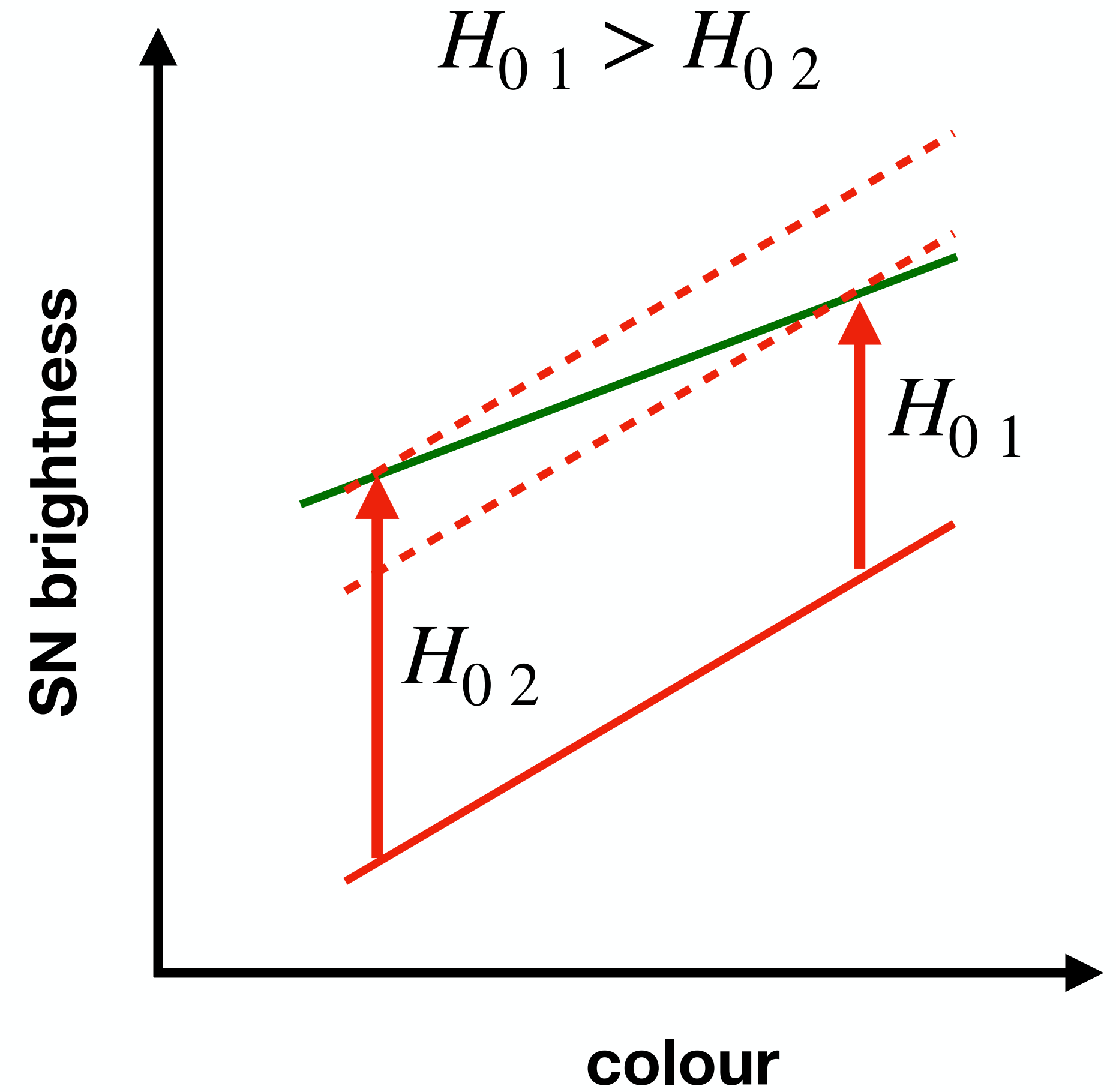
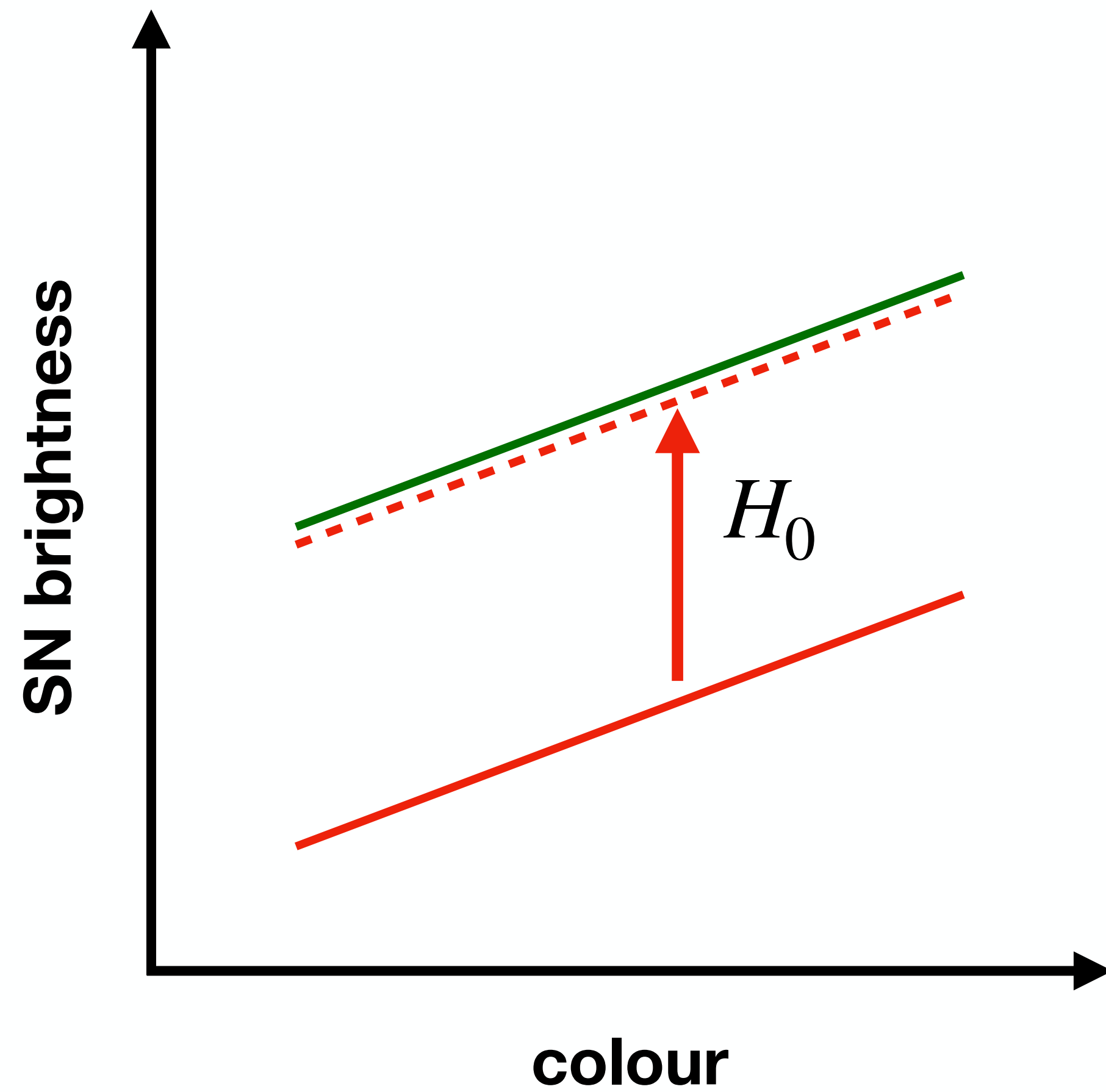
Calibration sample: $m_B = M_B - \alpha x_1 + \beta_{cal} c$

$\beta_{cal} > \beta !!$

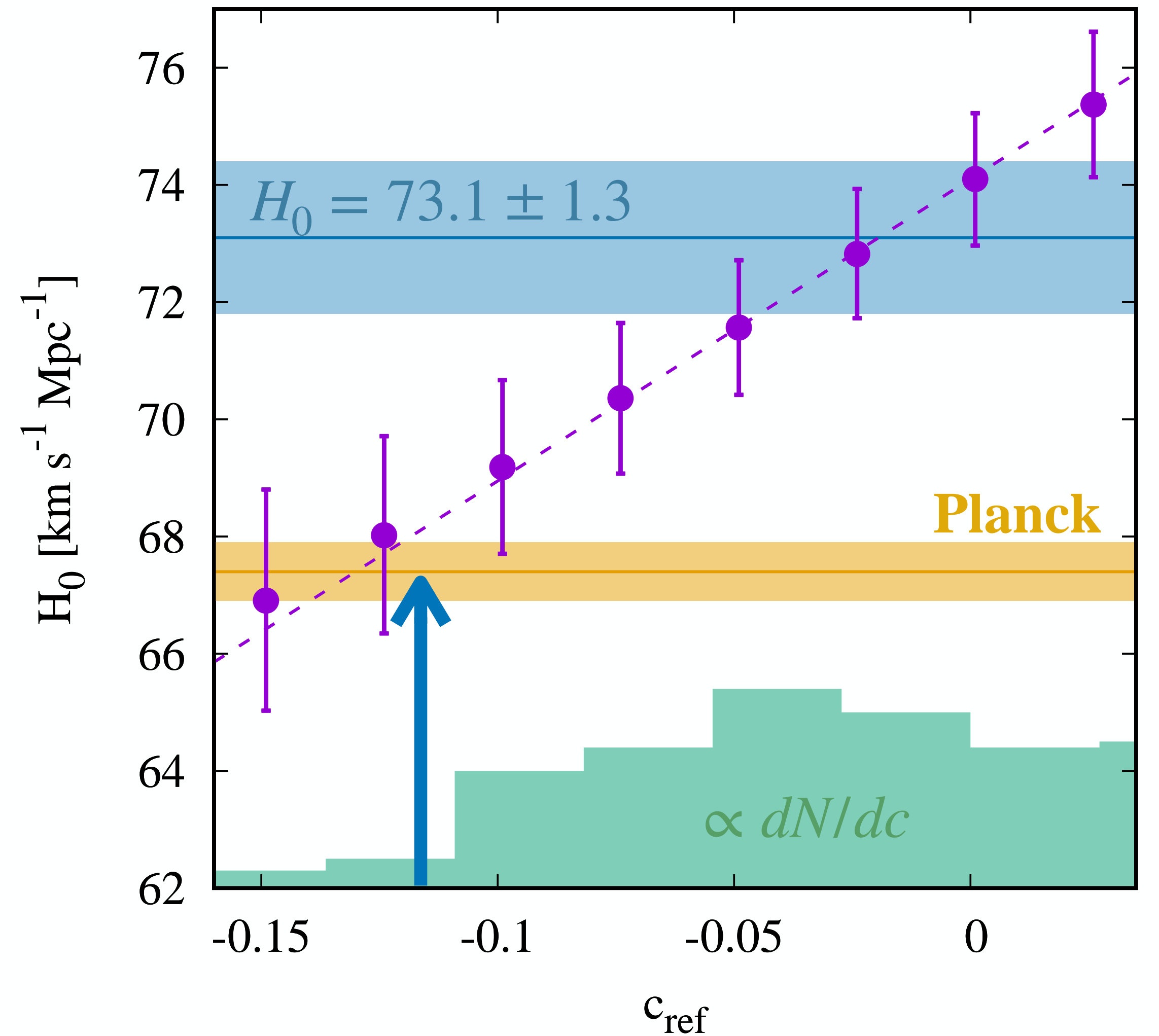
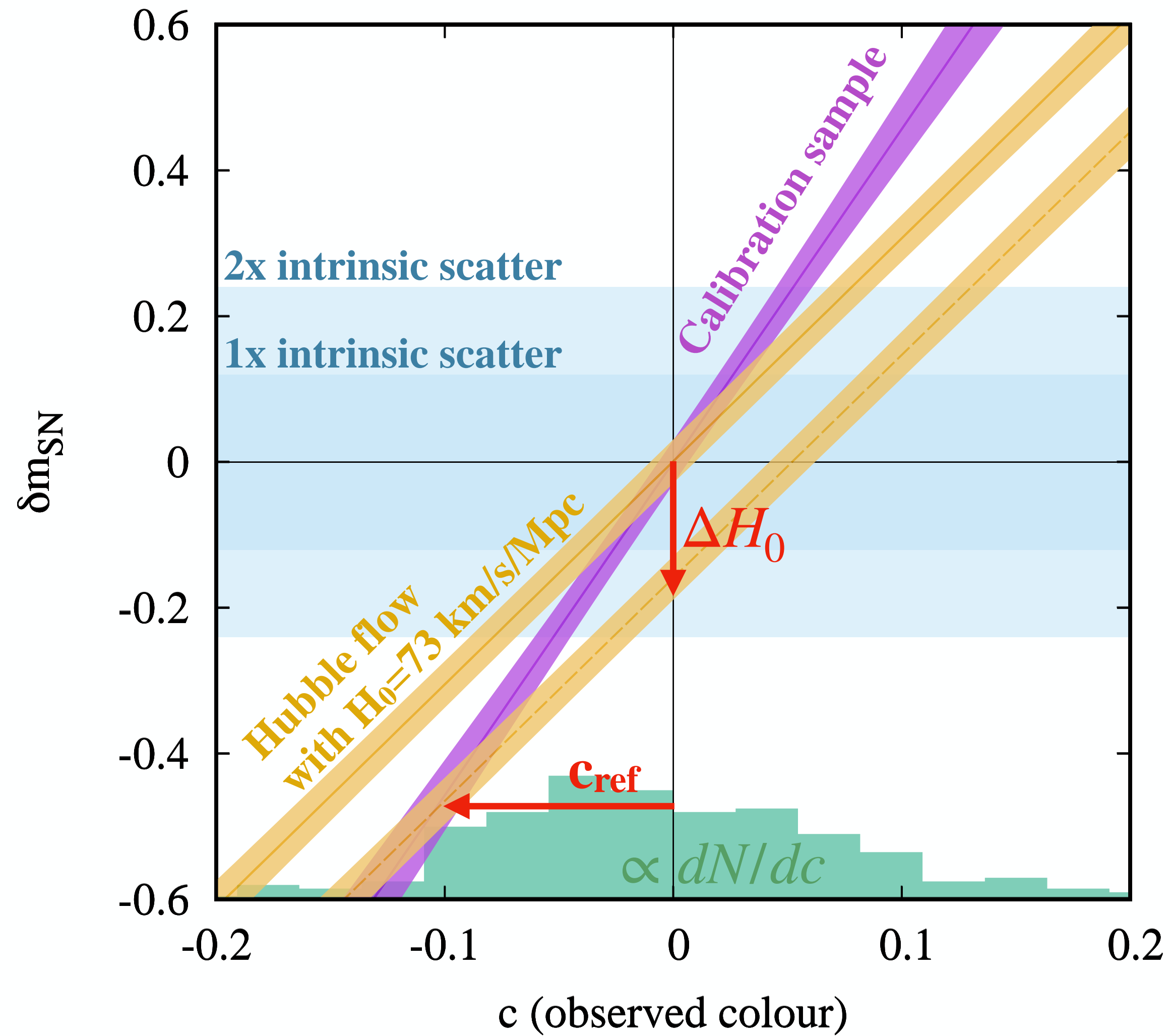
$\sigma_{int,cal} = 0 !!$

4.2σ (19 cal) Hubble constant tension
goes together with
 3.8σ intrinsic anomaly
of the SN standardisation.

Deriving H_0 : underdetermined problem

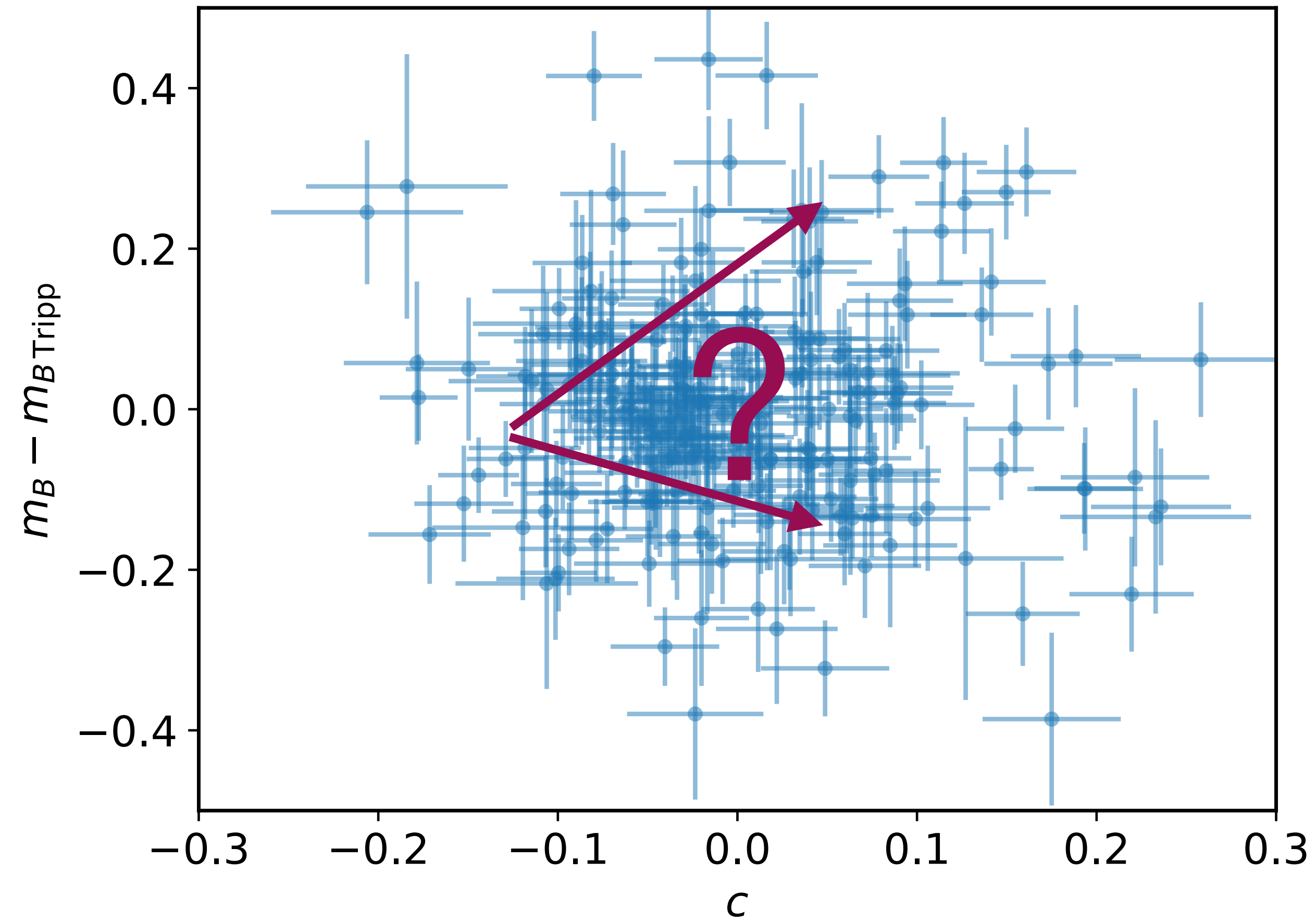
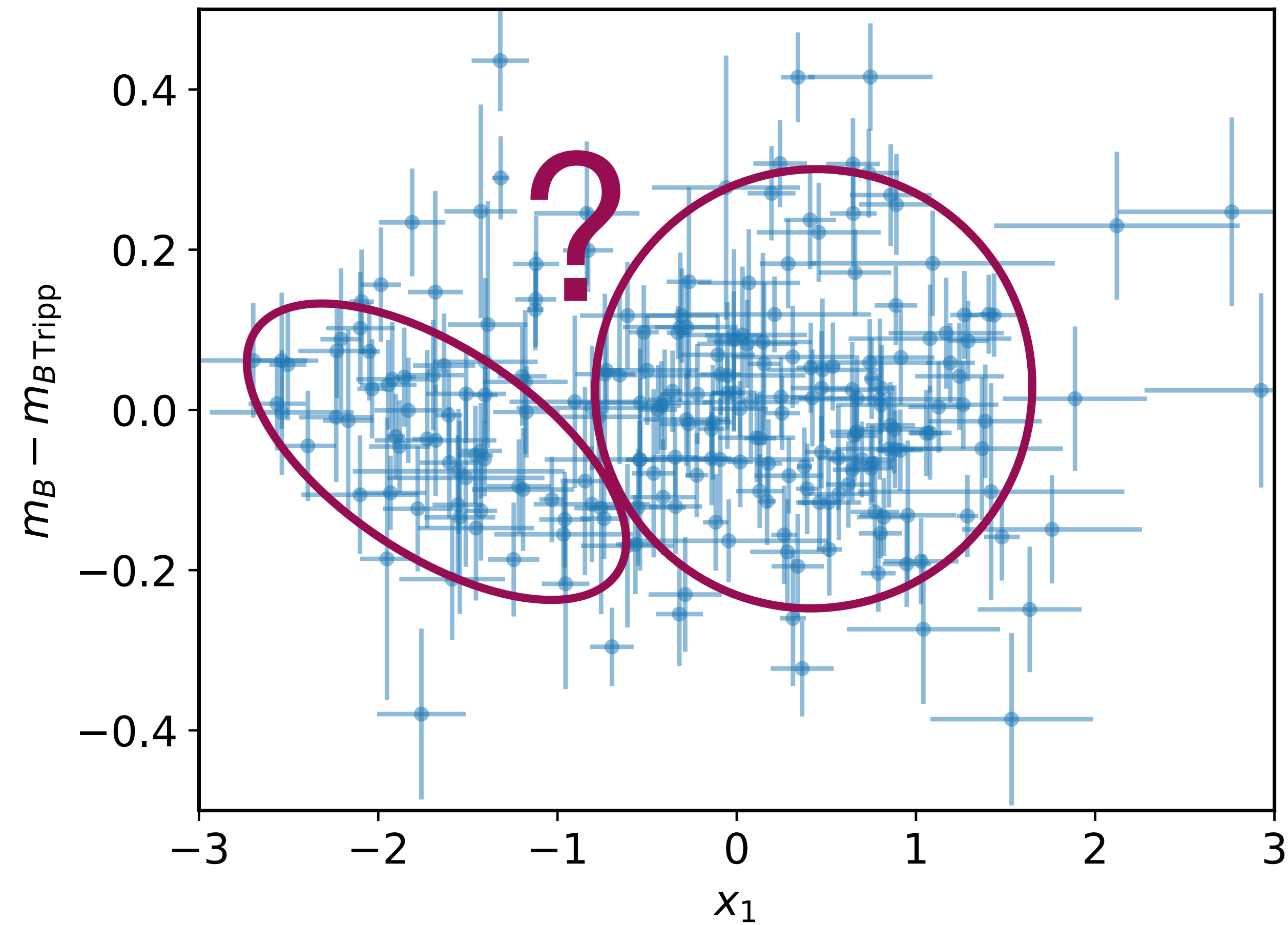


Hubble constant determination : proof-of-concept

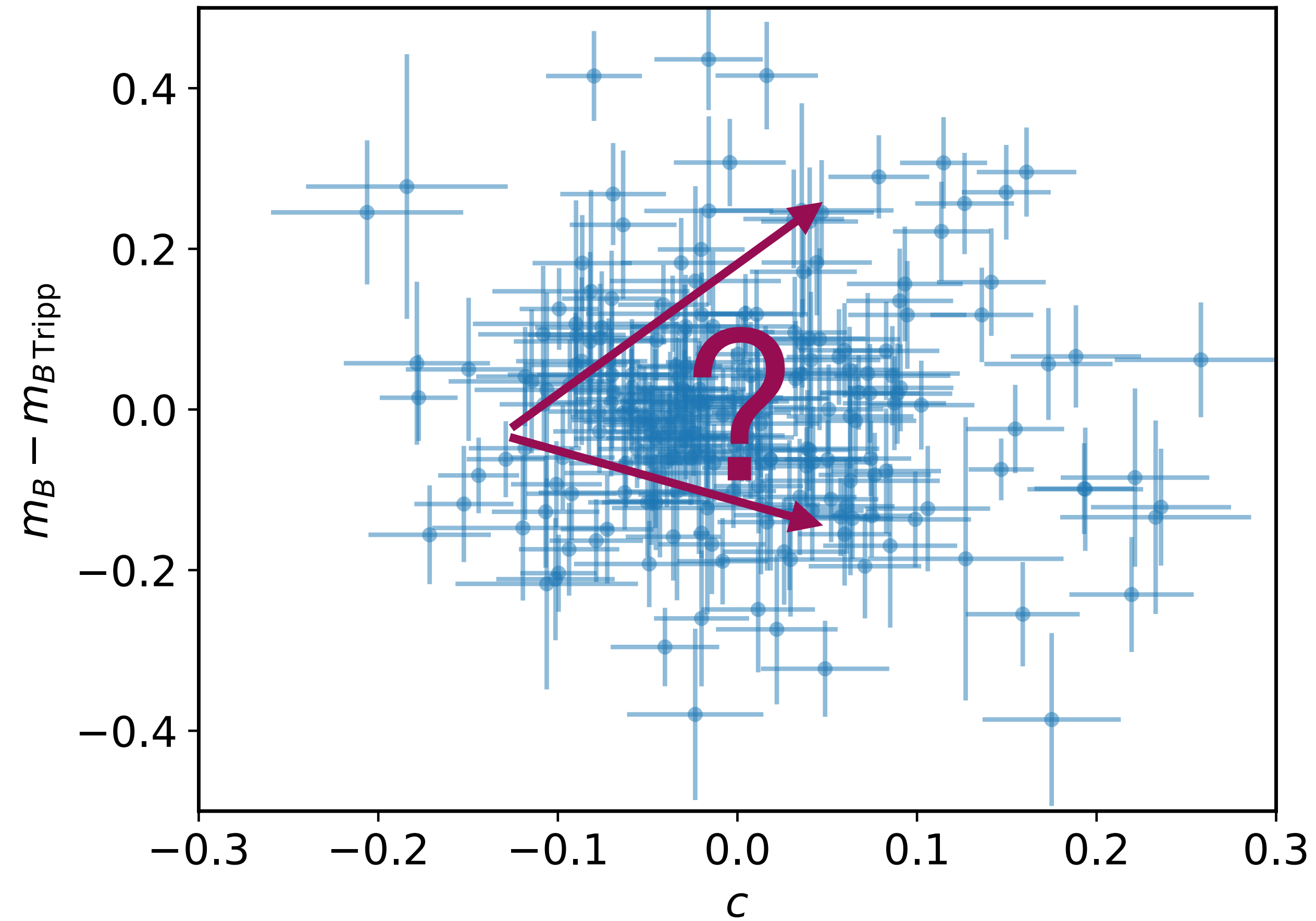
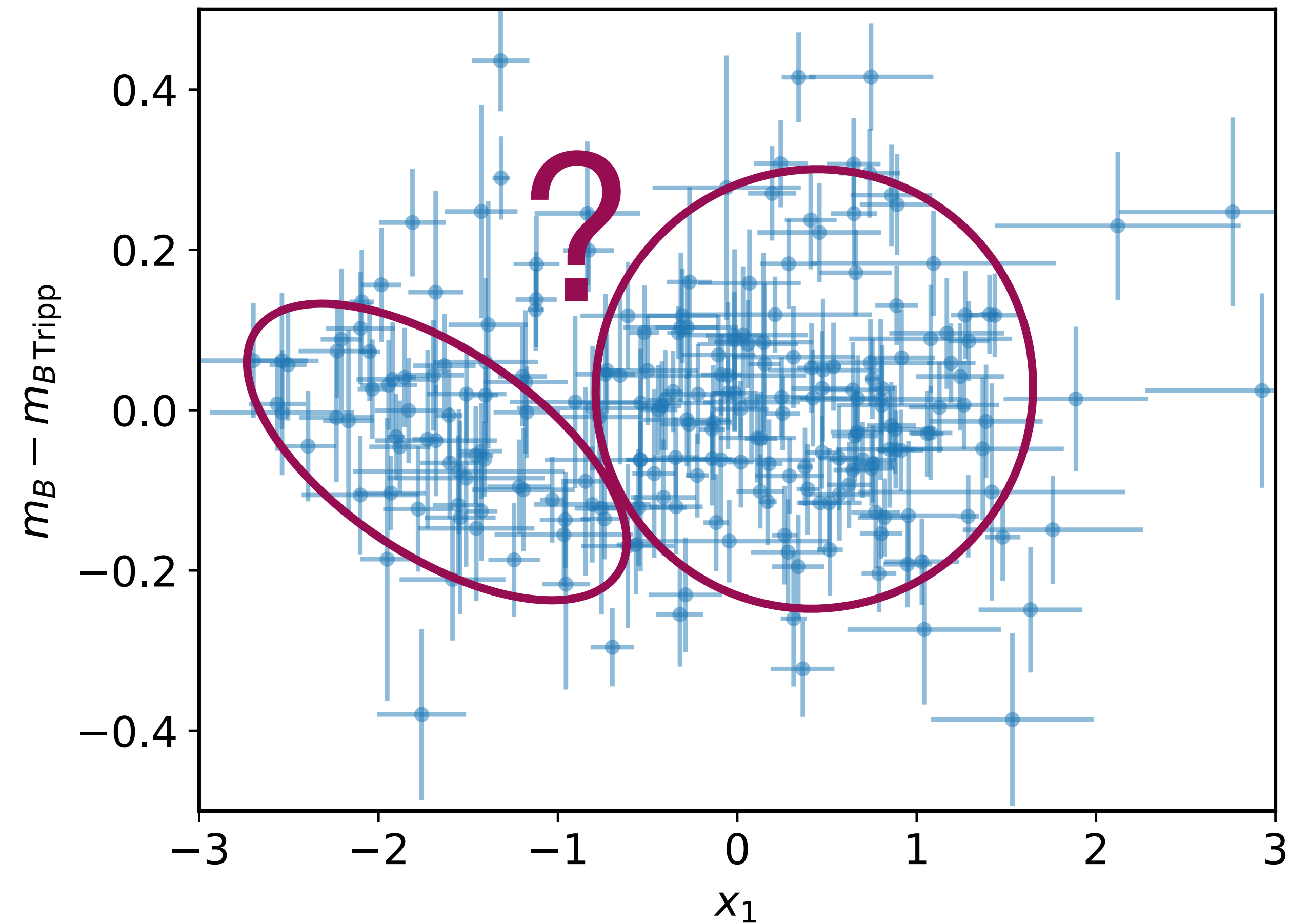


The local Hubble constant measurement
recovers the Planck value
when SN mag-colour relations
are matched at blue colours ($c \approx -0.12$).

The key is to understand Hubble residuals !

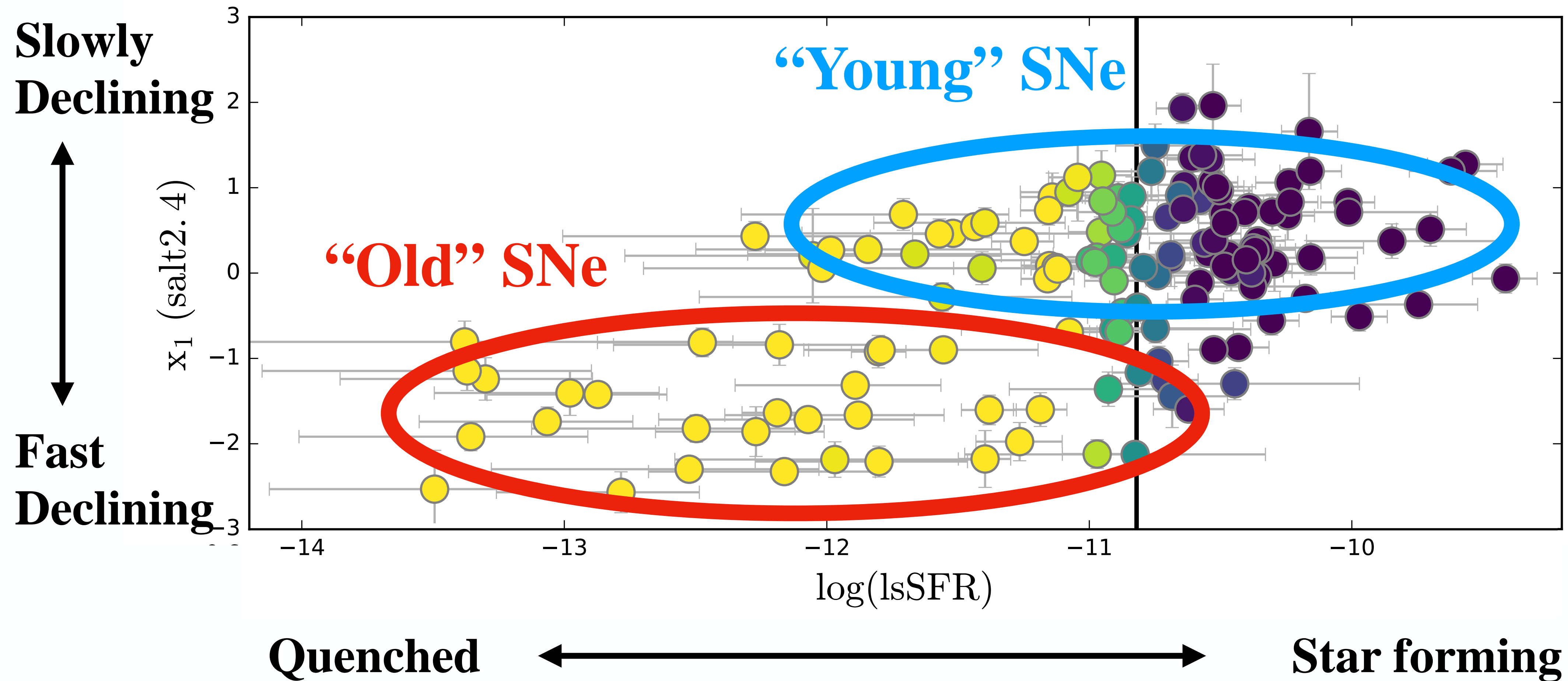


The key is to understand Hubble residuals !

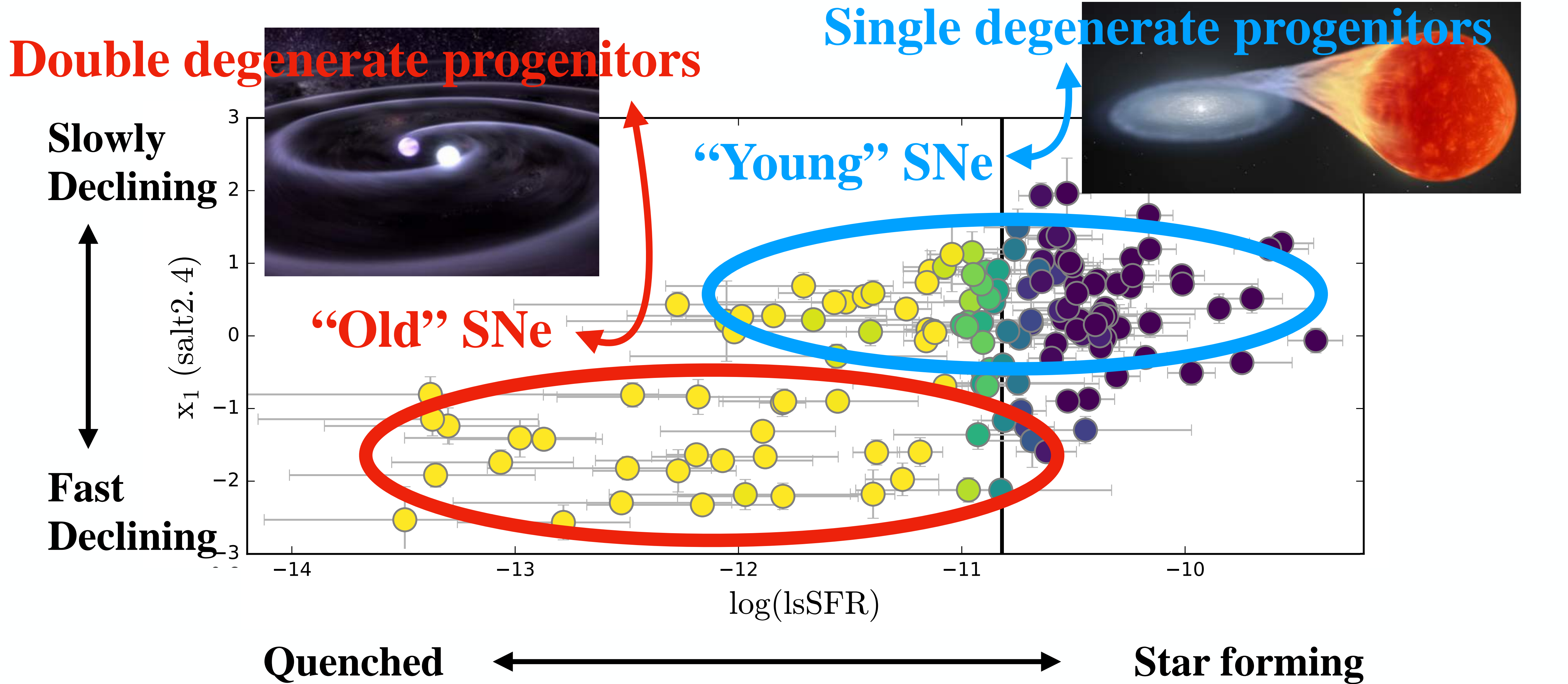


Dust: reddening, extinction
Mandel et al. (2017), Thorp et al. (2021),
Brout & Scolnic (2020)

SN populations

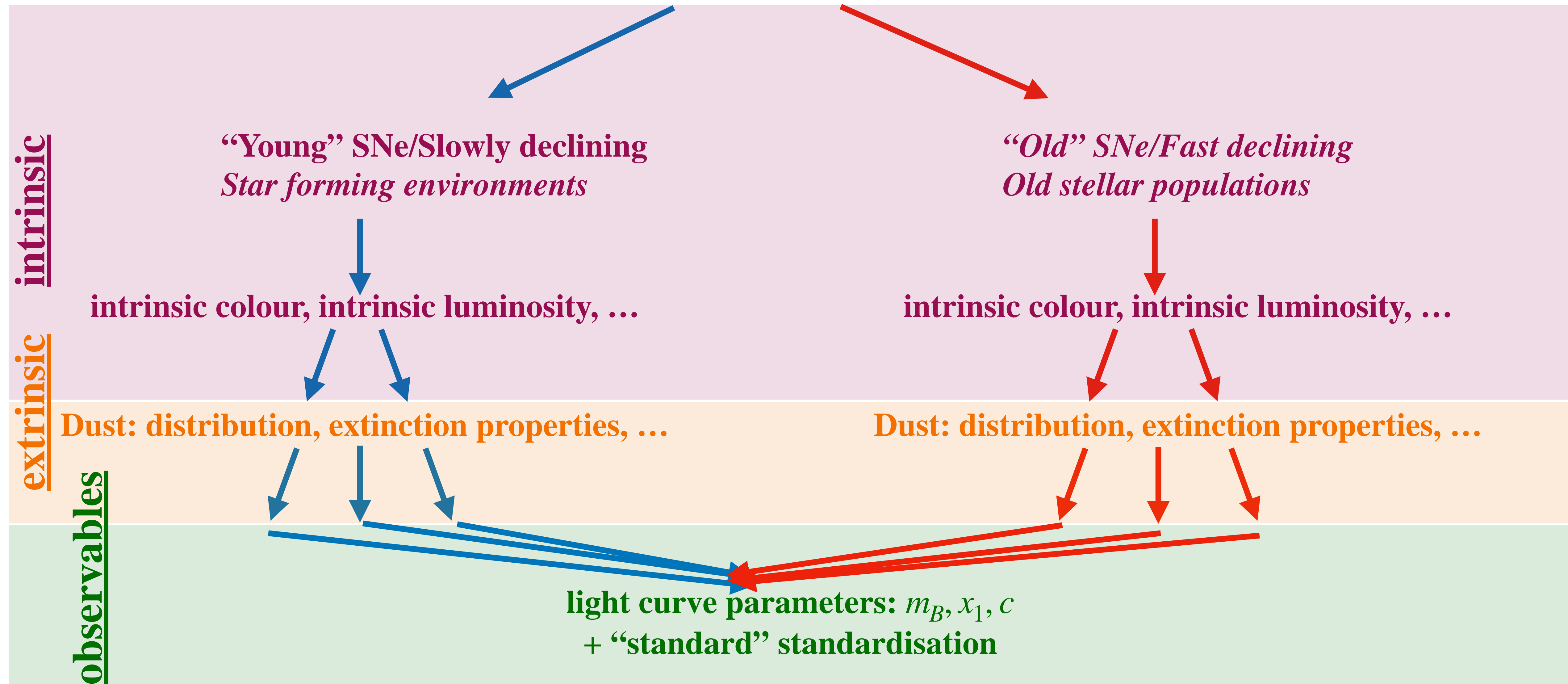


SN populations



Physically motivated model: flow chart

Type Ia SNe



Two-population bayesian hierarchical model

observables

latent variables (LV) \Rightarrow priors \Leftarrow hyperparameters

$$m_B = M_B + \mu + \alpha c_{\text{int}} + \beta X_1 + R_B E(B - V)$$

$$c = c_{\text{int}} + E(B - V)$$

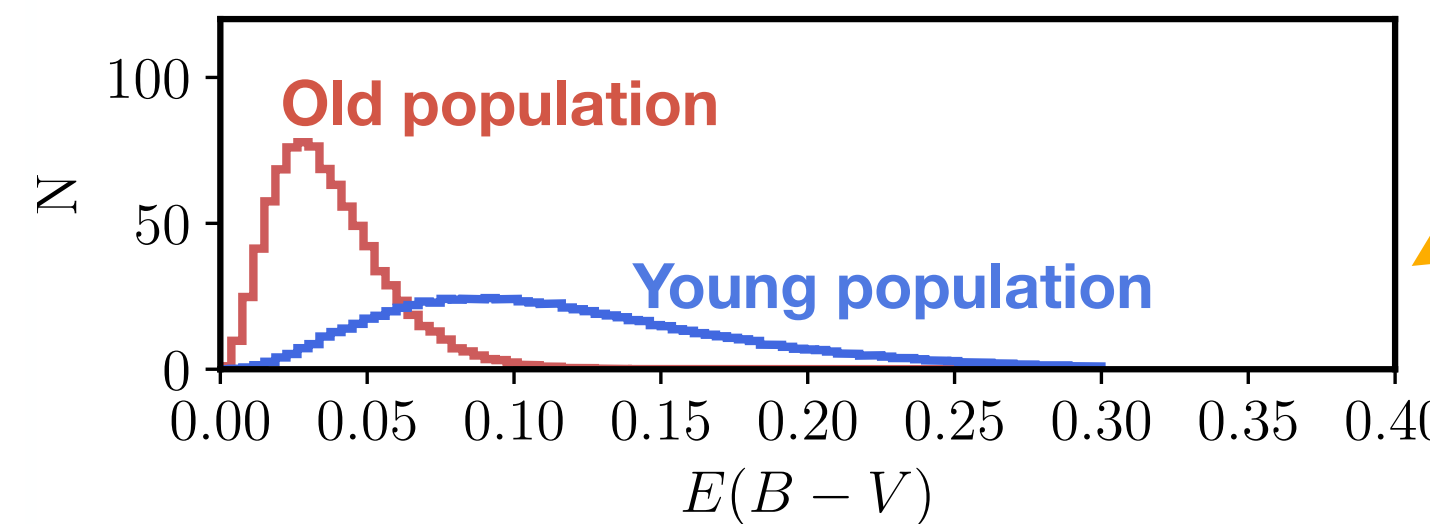
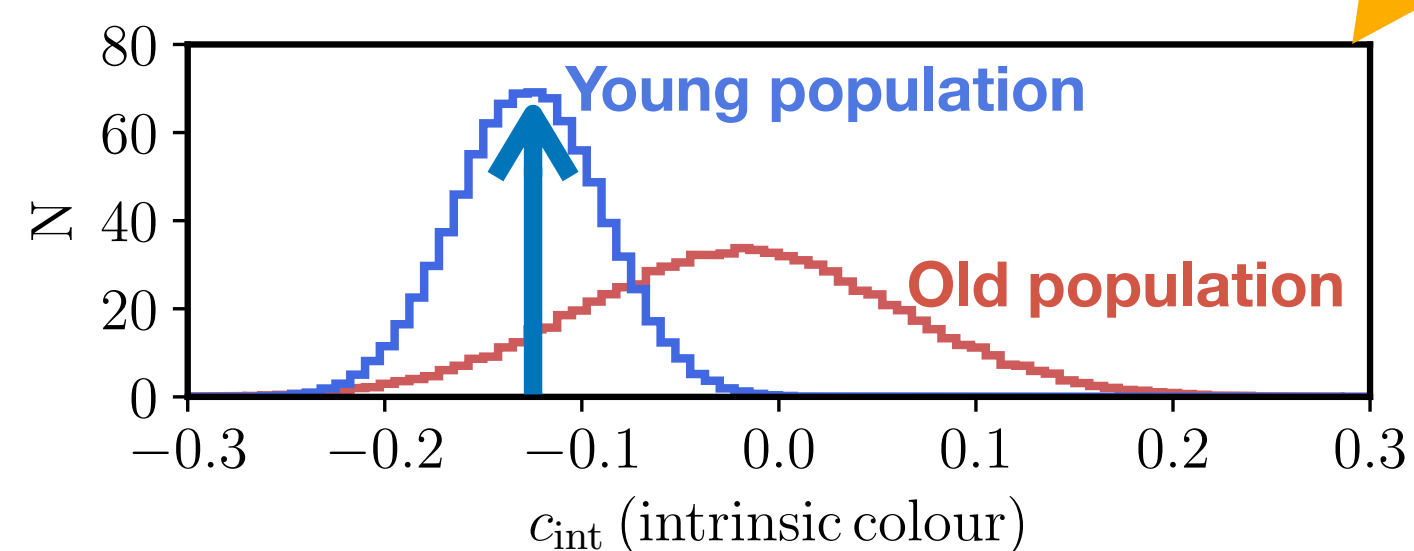
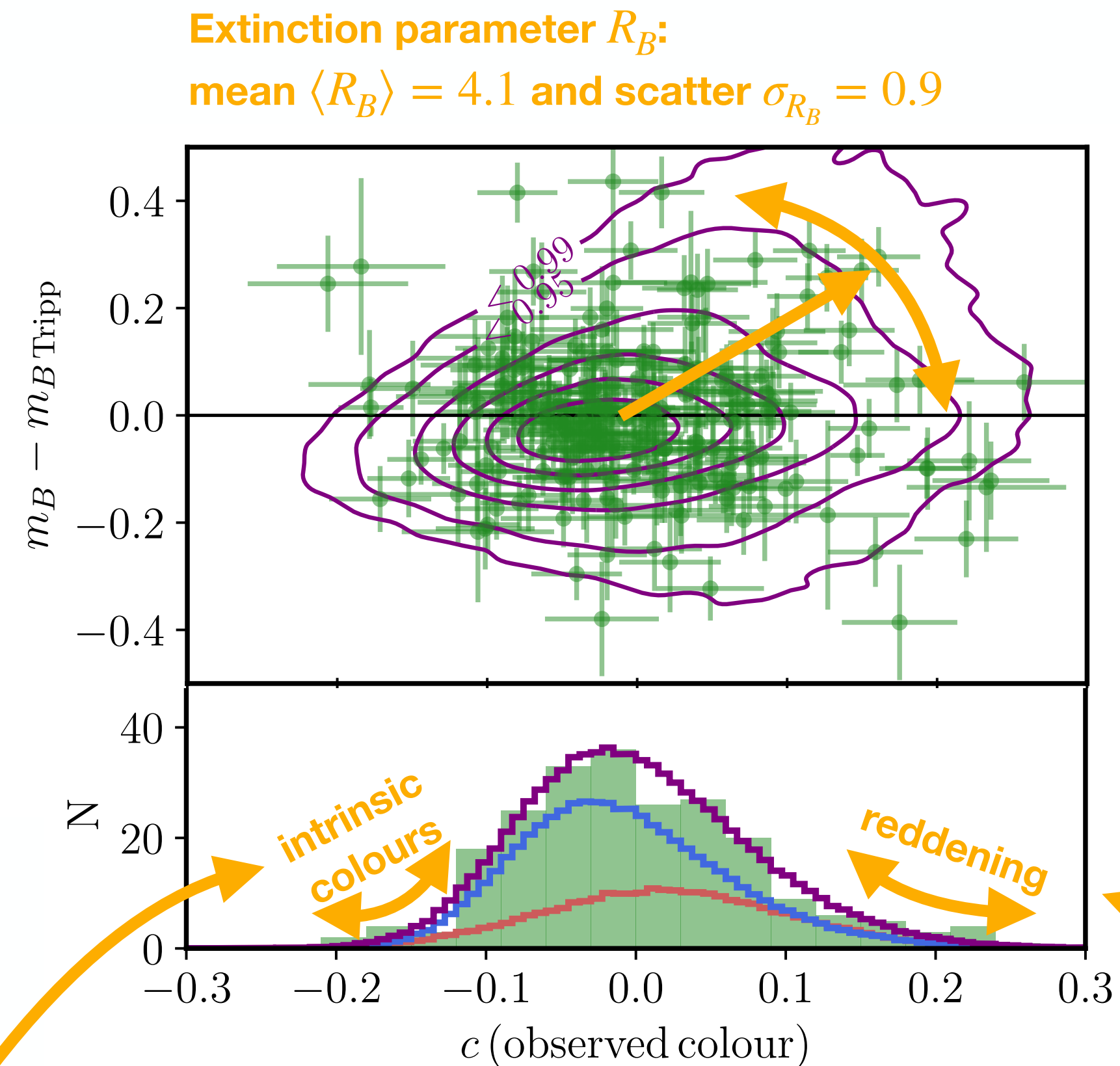
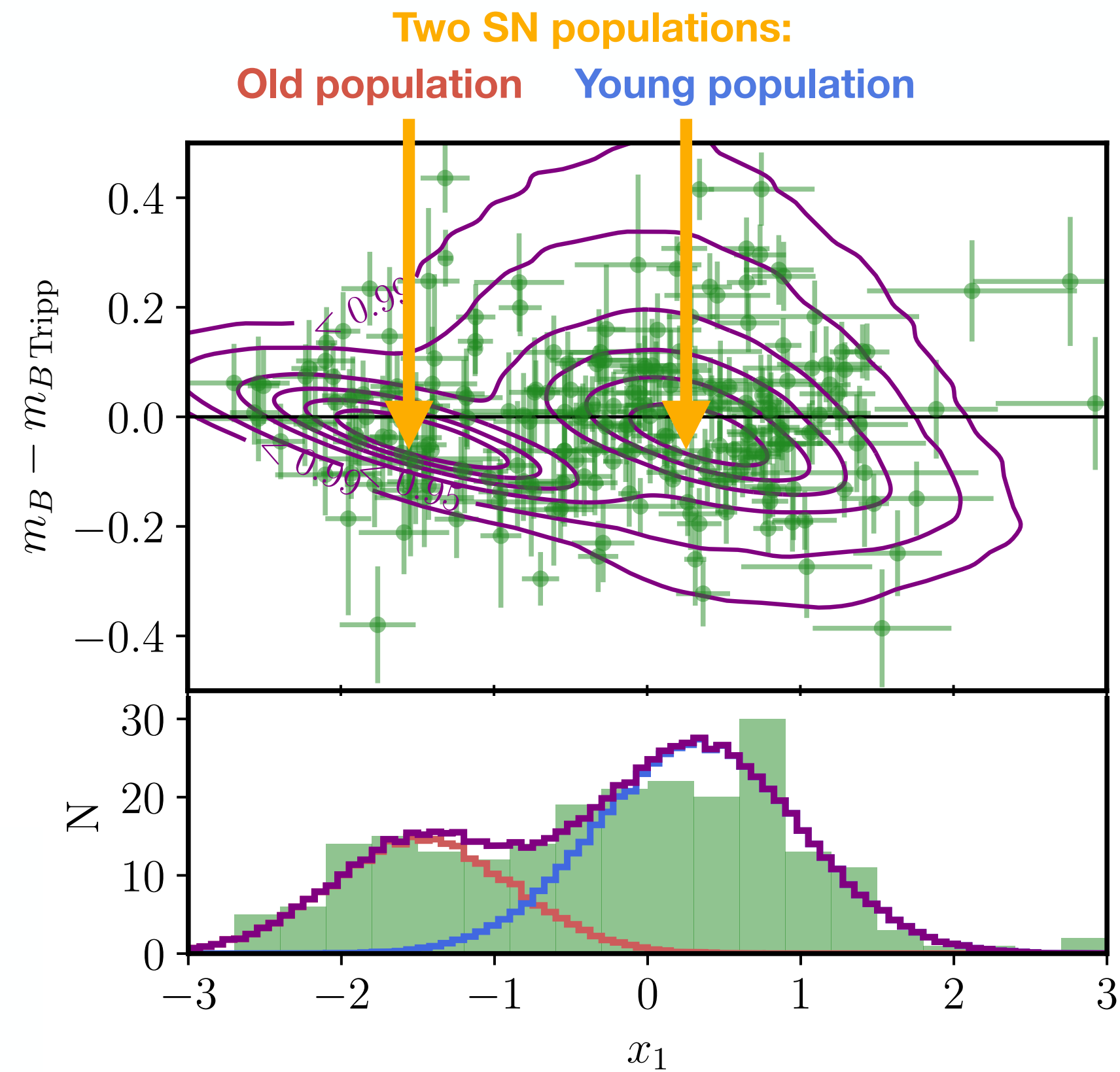
$$x_1 = X_1$$

Two sets of priors
(hyperparameters)

Two SN populations

$$w_{\text{SN}} = \frac{N_{\text{old population}}}{N_{\text{young population}} + N_{\text{old population}}}$$

Forward modelling with 2-pop Bayesian hierarchical model: Complete description of SNe in the Hubble flow



Extrinsic properties (↑): Are they different in the calibration sample ?

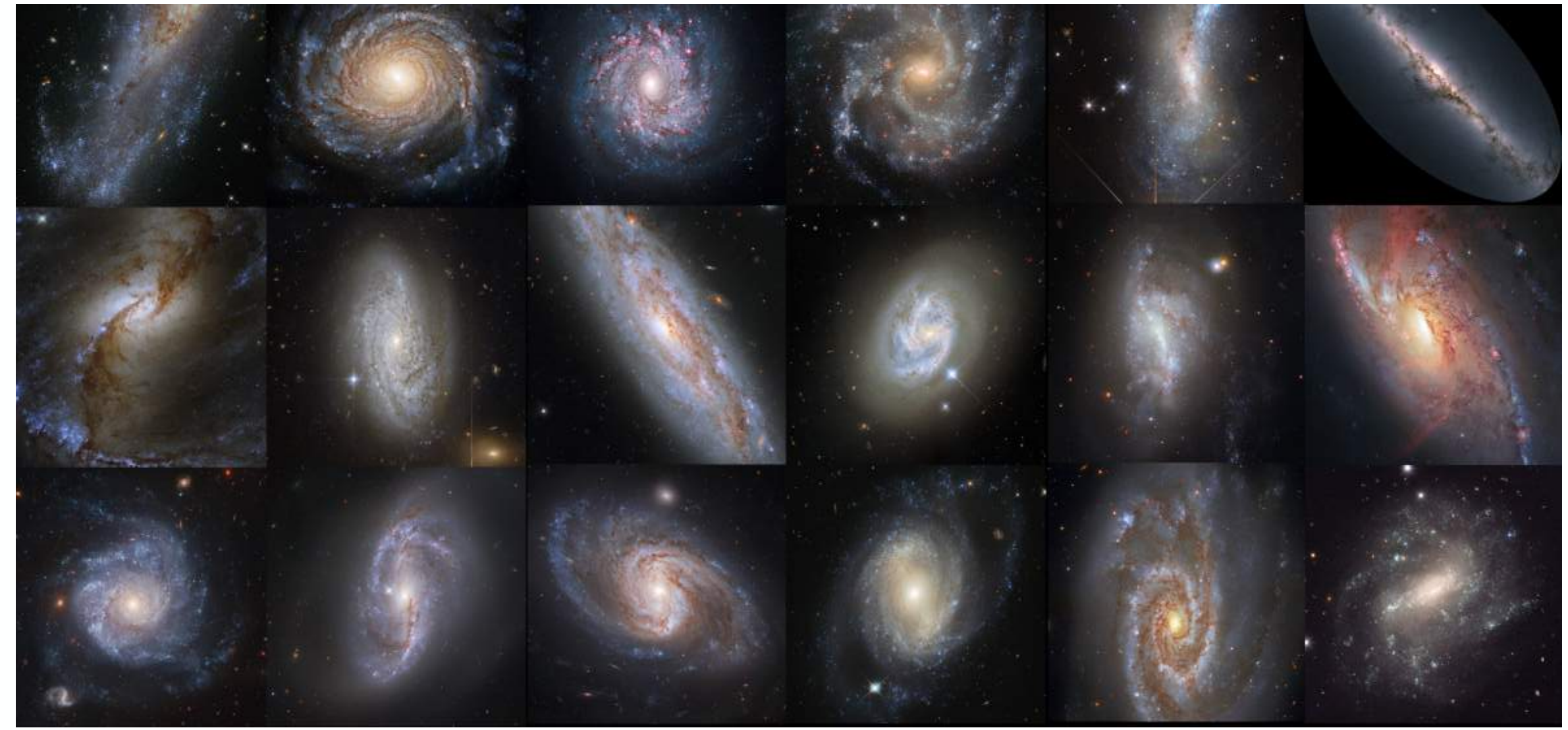
observables

latent variables (LV) \Rightarrow priors \Leftarrow hyperparameters

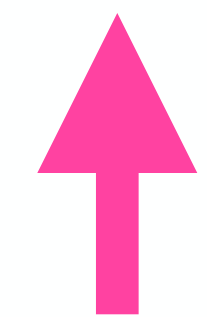
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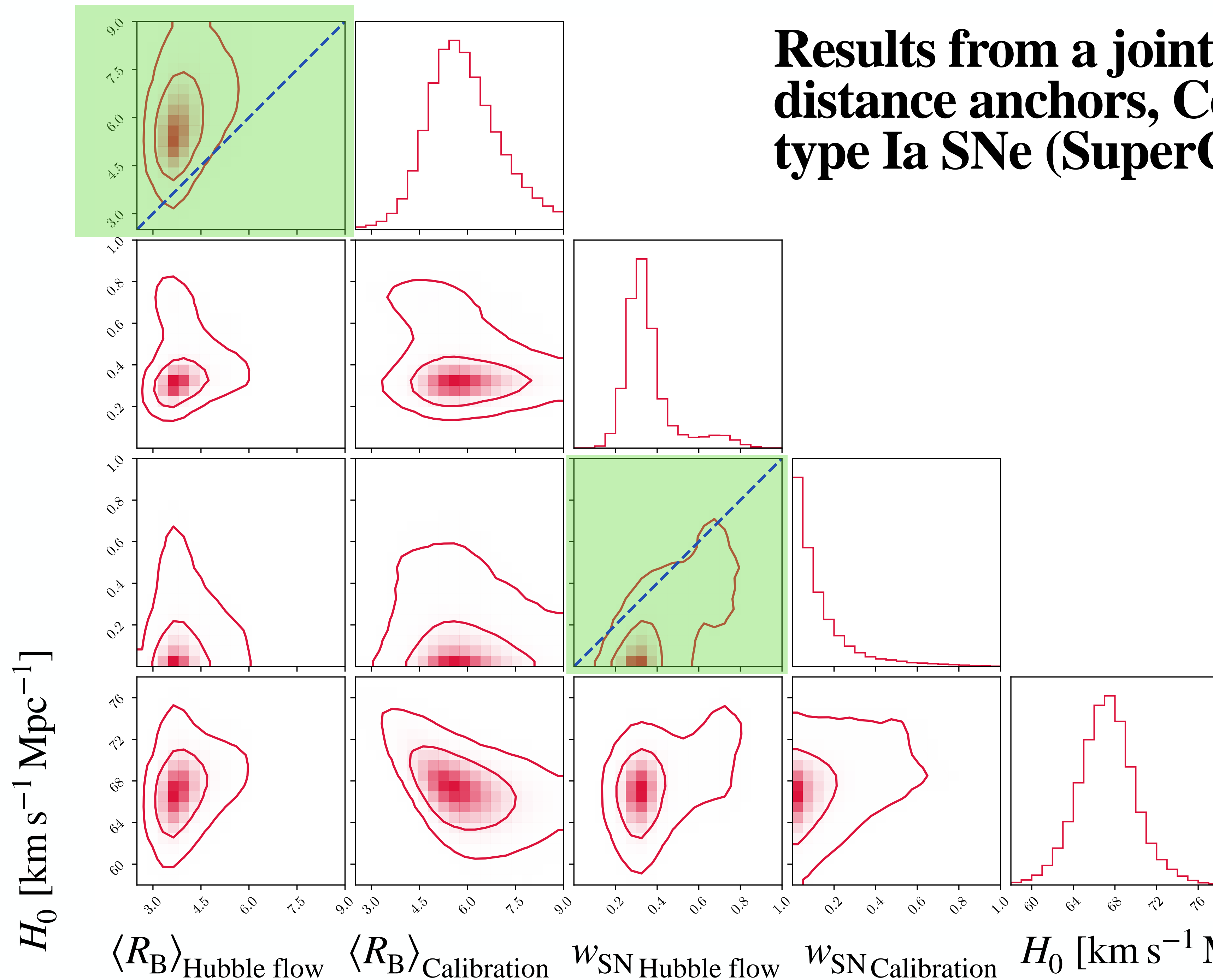
$$x_1 = X_1$$



$$w_{\text{SN}} = \frac{N_{\text{old population}}}{N_{\text{young population}} + N_{\text{old population}}}$$

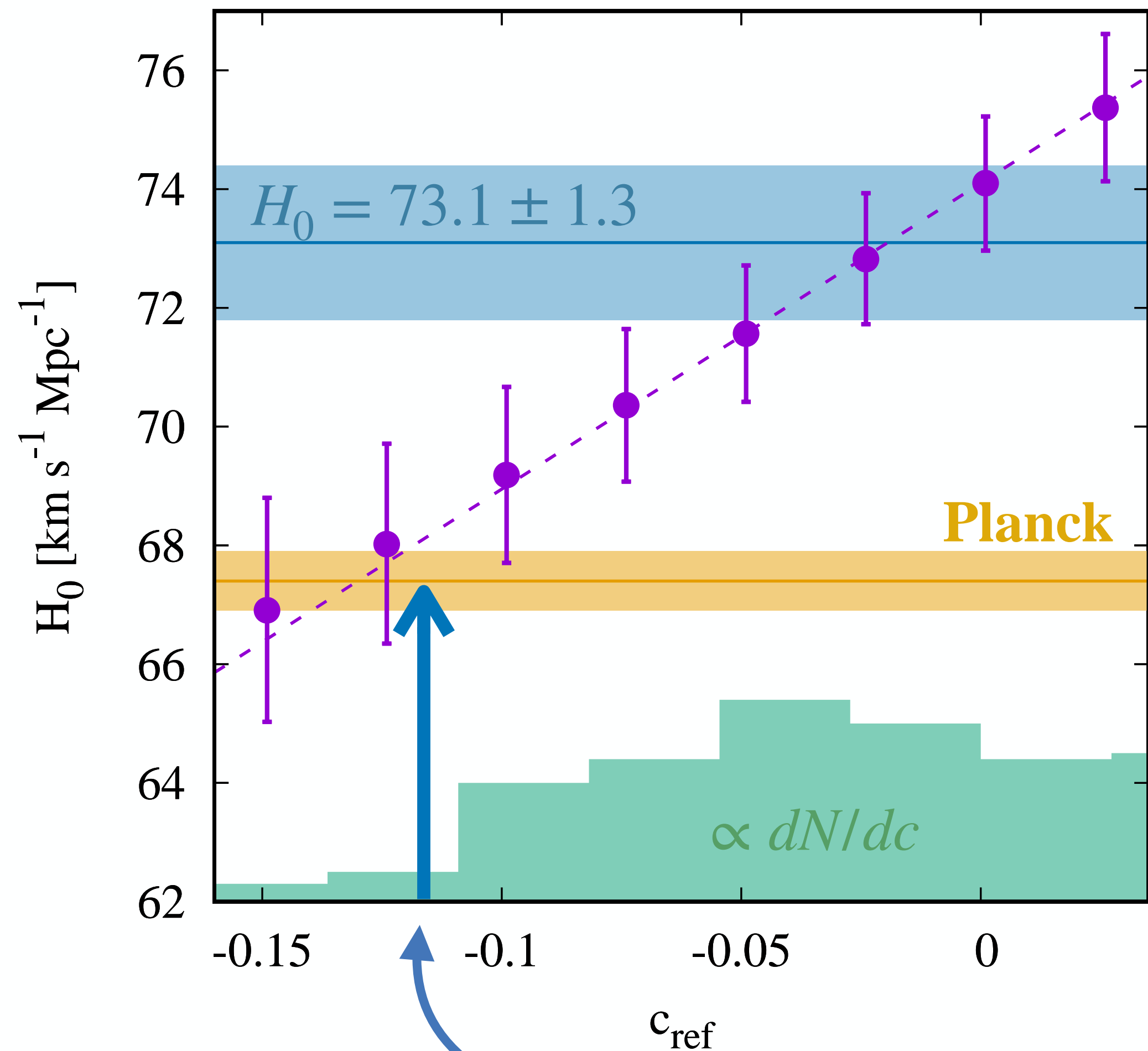


Results from a joint fit to SH0ES data: distance anchors, Cepheids (19 calibrators), type Ia SNe (SuperCal)



$$H_0 = 67.2^{+2.6}_{-2.6}$$

Intuitive interpretation



Higher (mean) extinction parameter in the calibration sample than in the Hubble flow

Intrinsic colours of young supernova population dominating in the calibration sample

New Hubble constant

Tripp calibration

$$H_0 = 73.1^{+1.3}_{-1.3}$$

2-pop model:

The same params in the calibration
and Hubble flow

$$H_0 = 72.4^{+1.2}_{-1.2}$$

2-pop model:

independent $\langle R_B \rangle$, σ_{R_B} , $\langle E(B - V) \rangle$, w
in the calibration and Hubble flow

$$H_0 = 67.2^{+2.6}_{-2.6}$$

2-pop model:

independent $\langle R_B \rangle$, w (and $\sigma_{R_B} = 0$)
in the calibration and Hubble flow

$$H_0 = 66.9^{+2.4}_{-2.4}$$

Physically motivated analysis
of type Ia supernovae
based on 2-population Bayesian
hierarchical model
resolves the Hubble constant tension.

Summary

- 4.2σ Hubble constant tension goes together 3.8σ intrinsic anomaly of the SN standardisation (19 calibrators).

RW & Hjorth (2022)

- Understanding the physical origin of the anomaly requires complete understanding of supernova Hubble residuals. The new two-population Bayesian hierarchical model provides for the first time the necessary framework.

RW, Hjorth & Hjortlund (2023)

- The new modelling of type Ia supernovae shows that the colour anomaly is caused by (1) a higher extinction parameter and (2) a larger fraction of “young” SN population in the calibration sample than in the Hubble flow.

- Reanalysis of the SH0ES data using the new 2-population model yields the Hubble constant which is fully consistent with the Planck value.

RW & Hjorth (2023) TBS

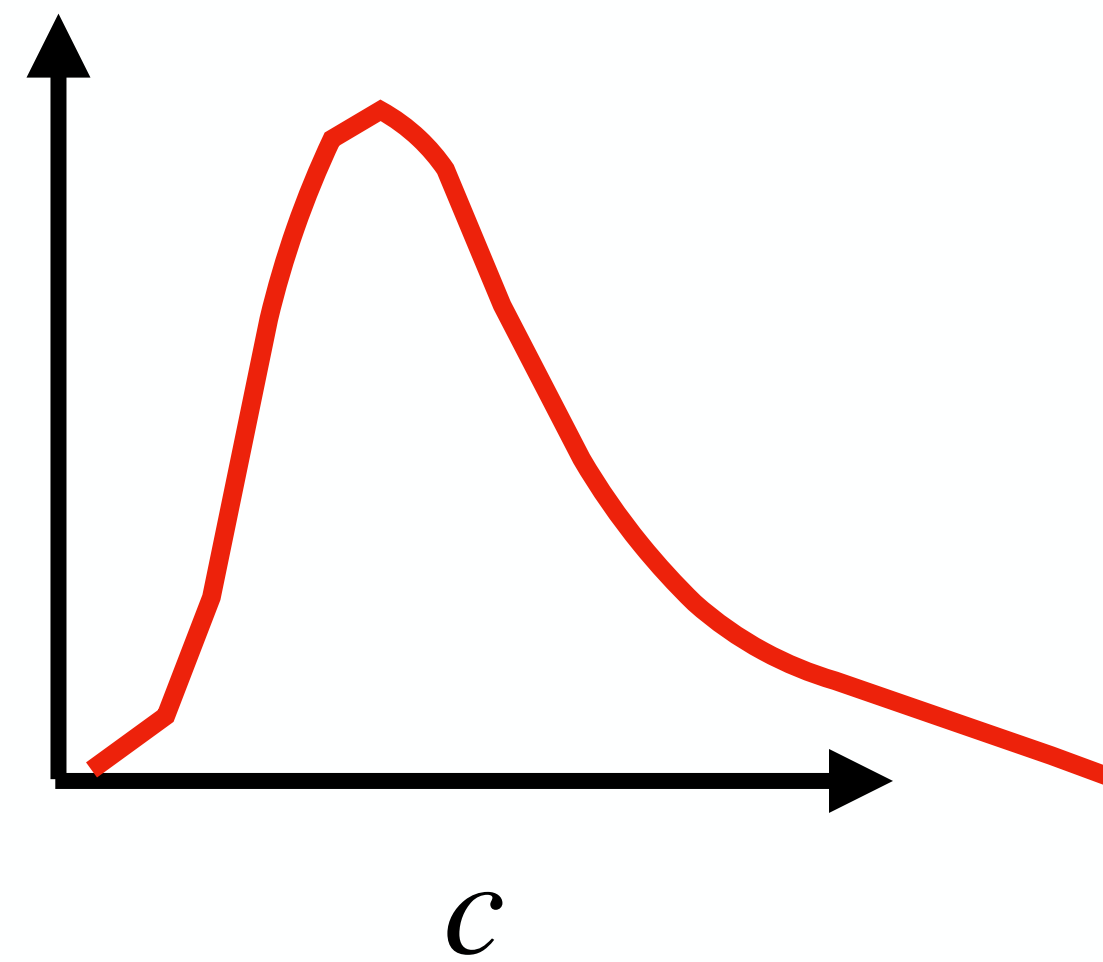
How does it work ?

observables **latent variables (LV) \Rightarrow priors \Leftarrow hyperparameters**

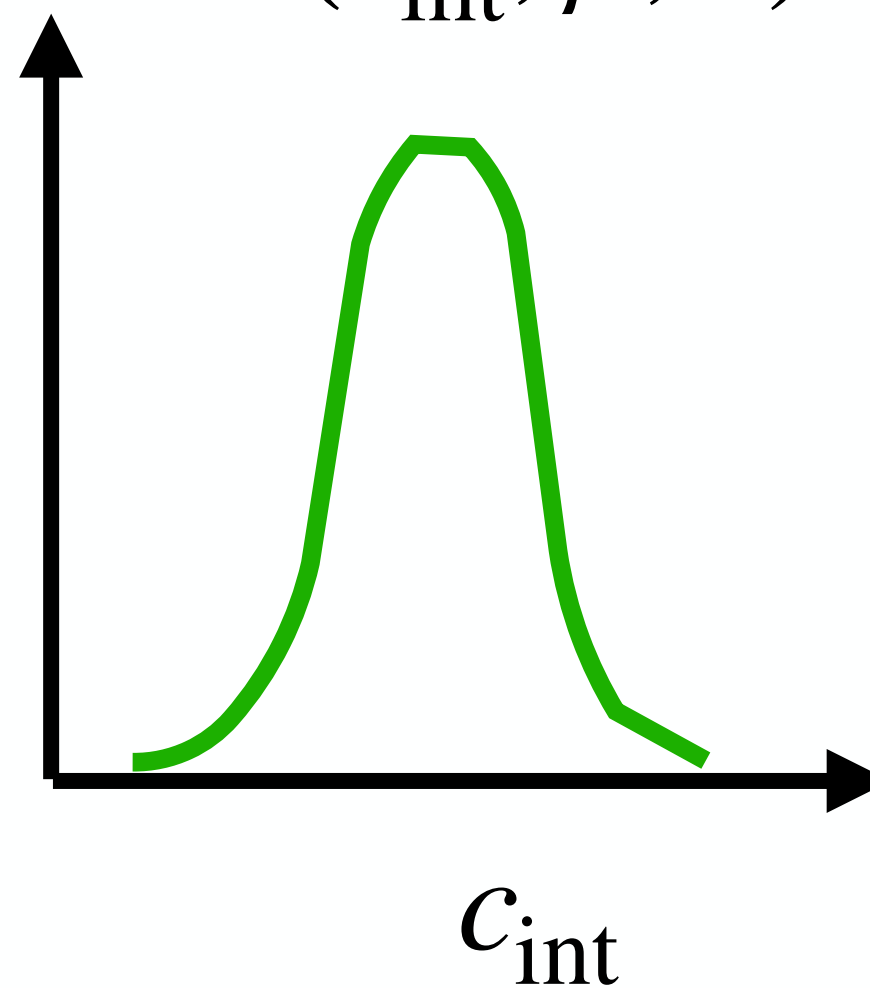
$$c = c_{\text{int}} + E(B - V)$$

$G(c_{\text{int}}; \mu, \sigma)$

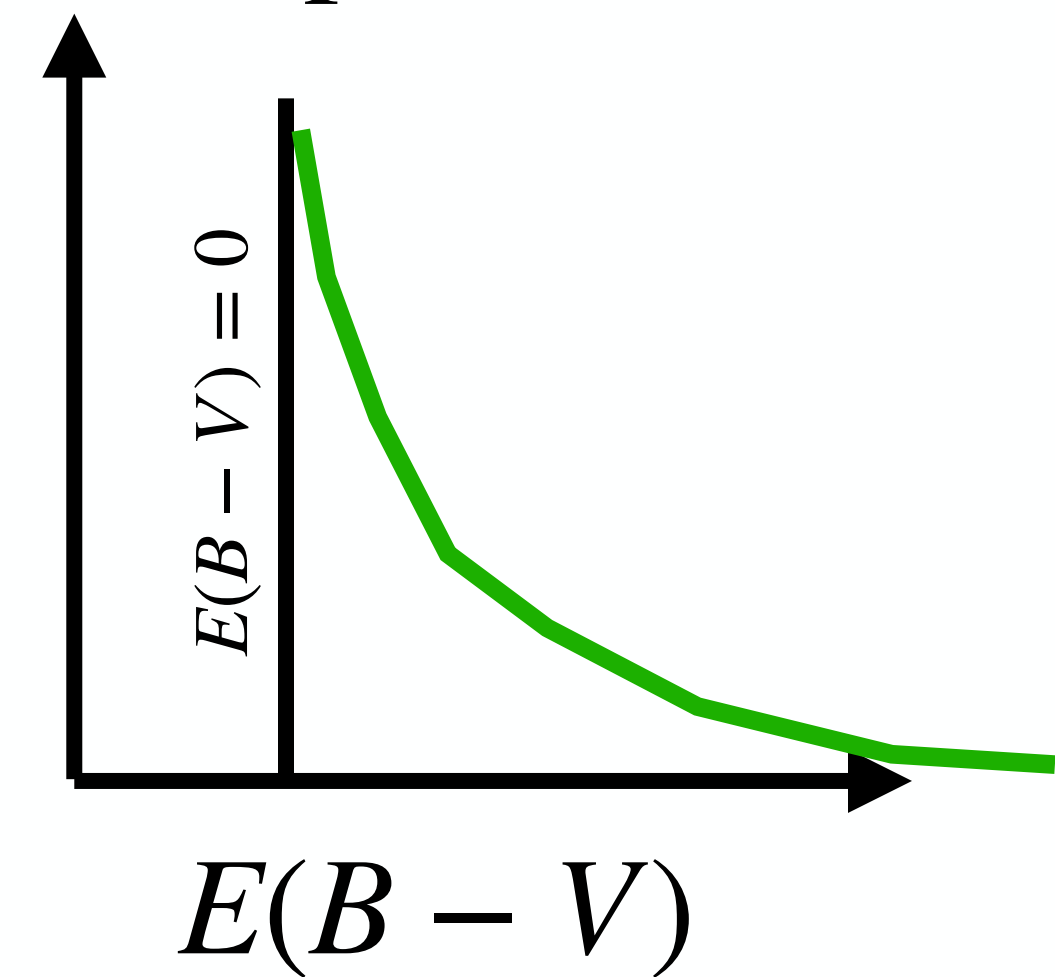
Exponential or (Gamma)



$=$



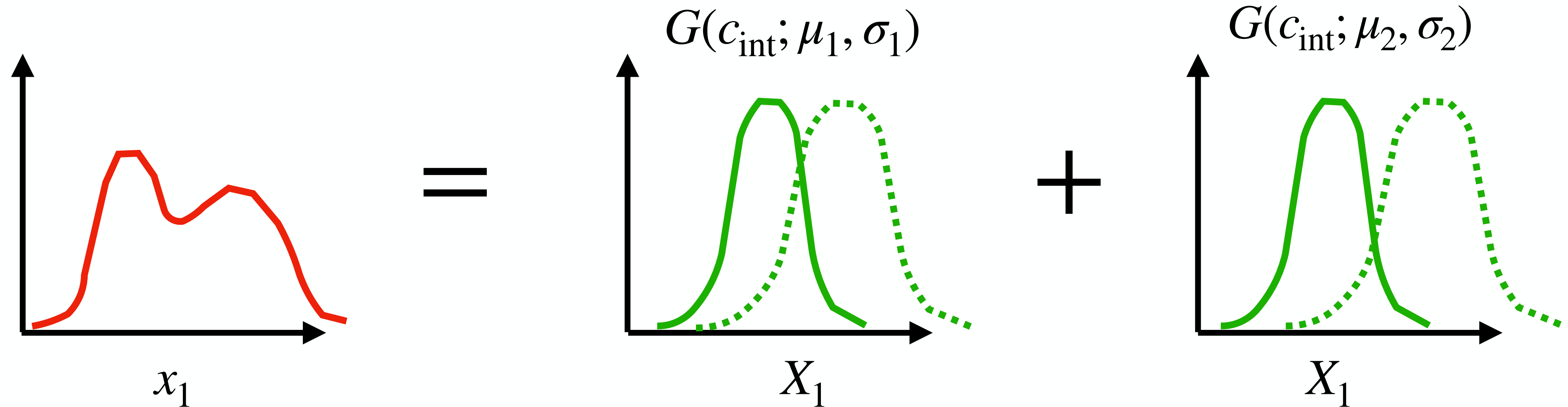
$*$



How does it work ?

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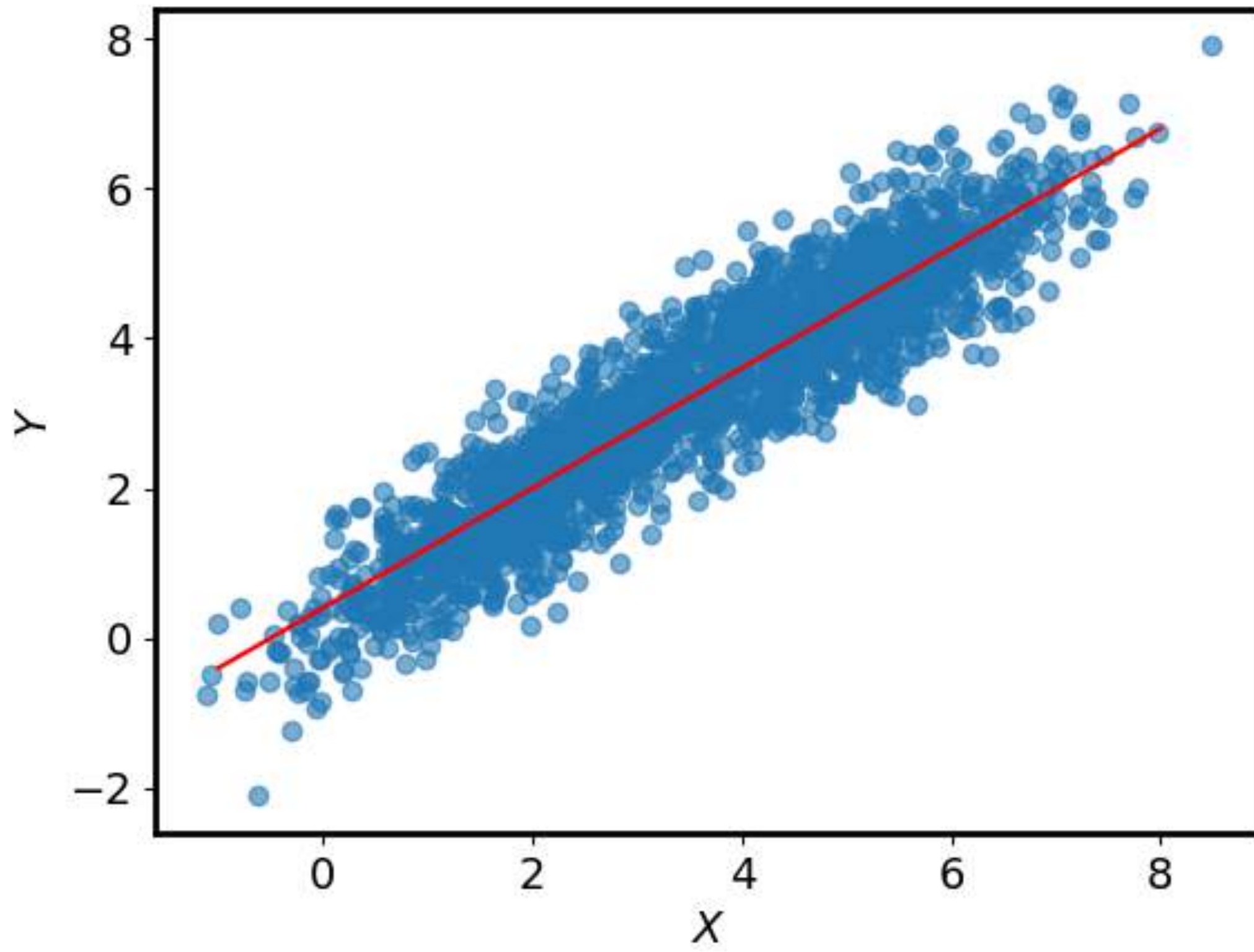
$$x_1 = X_1$$



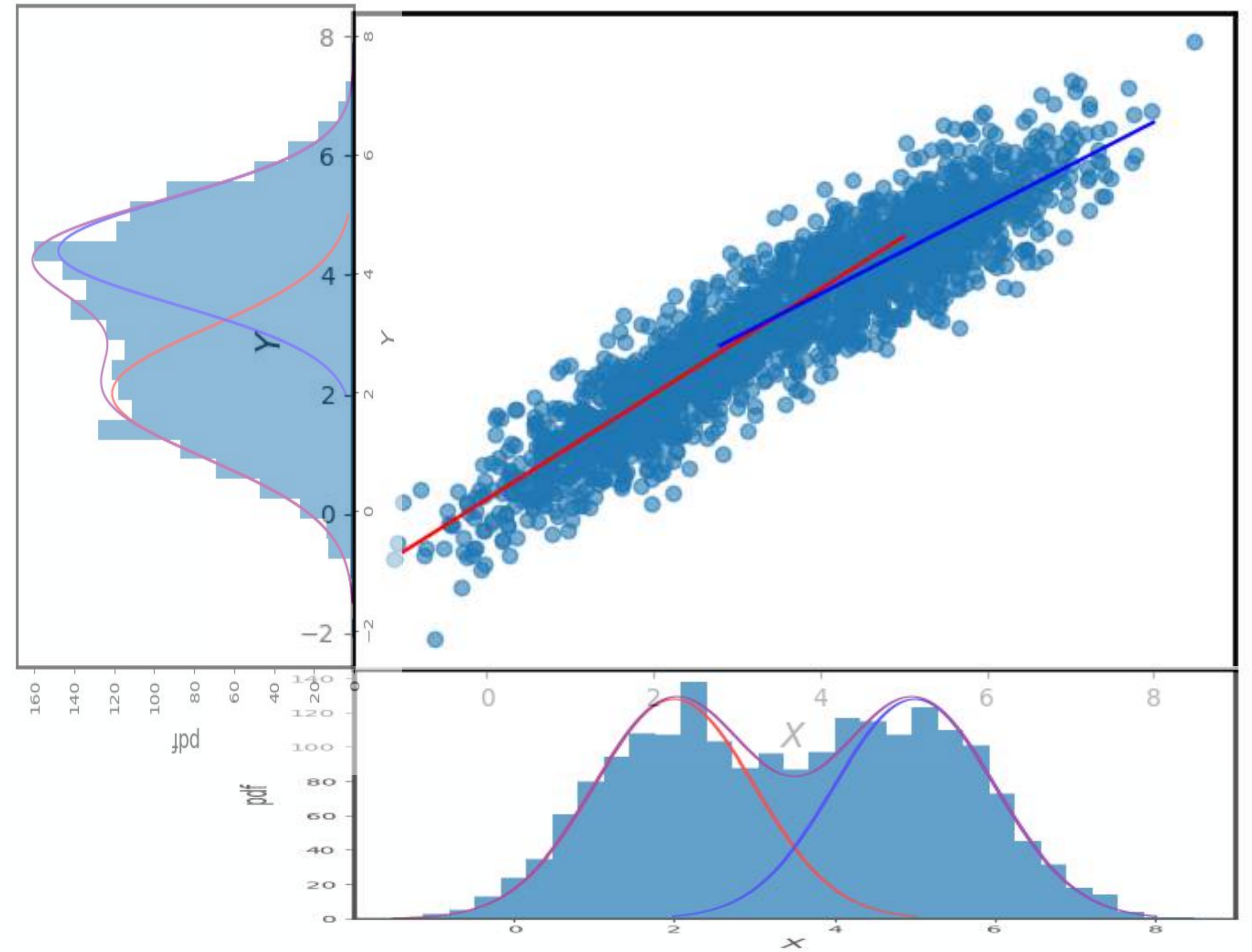
Bayesian hierarchical modelling

How does it work ?

Traditional modelling:
Relations between observables

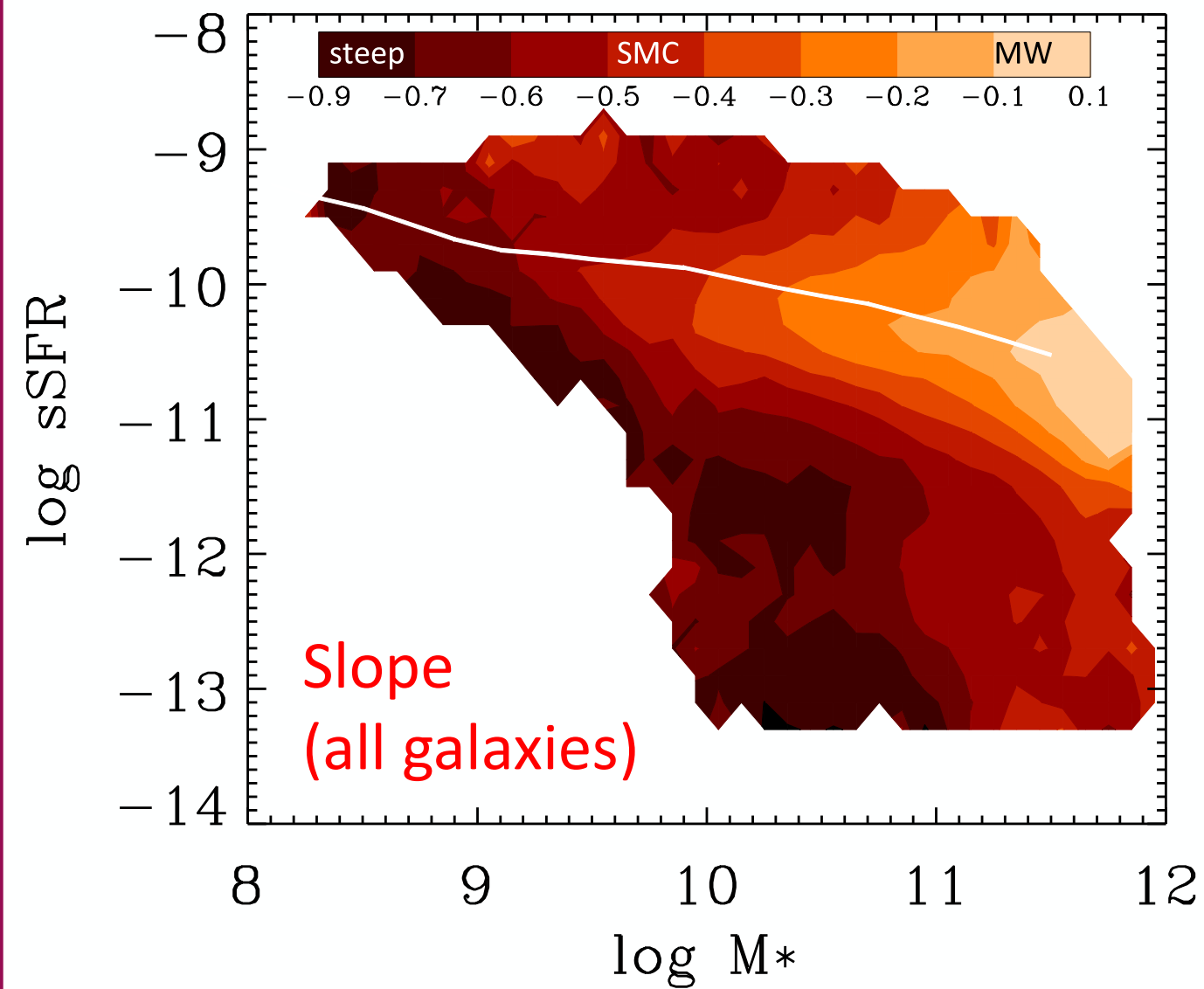


Bayesian hierarchical modelling:
Relations between observables+distribution of
Observables



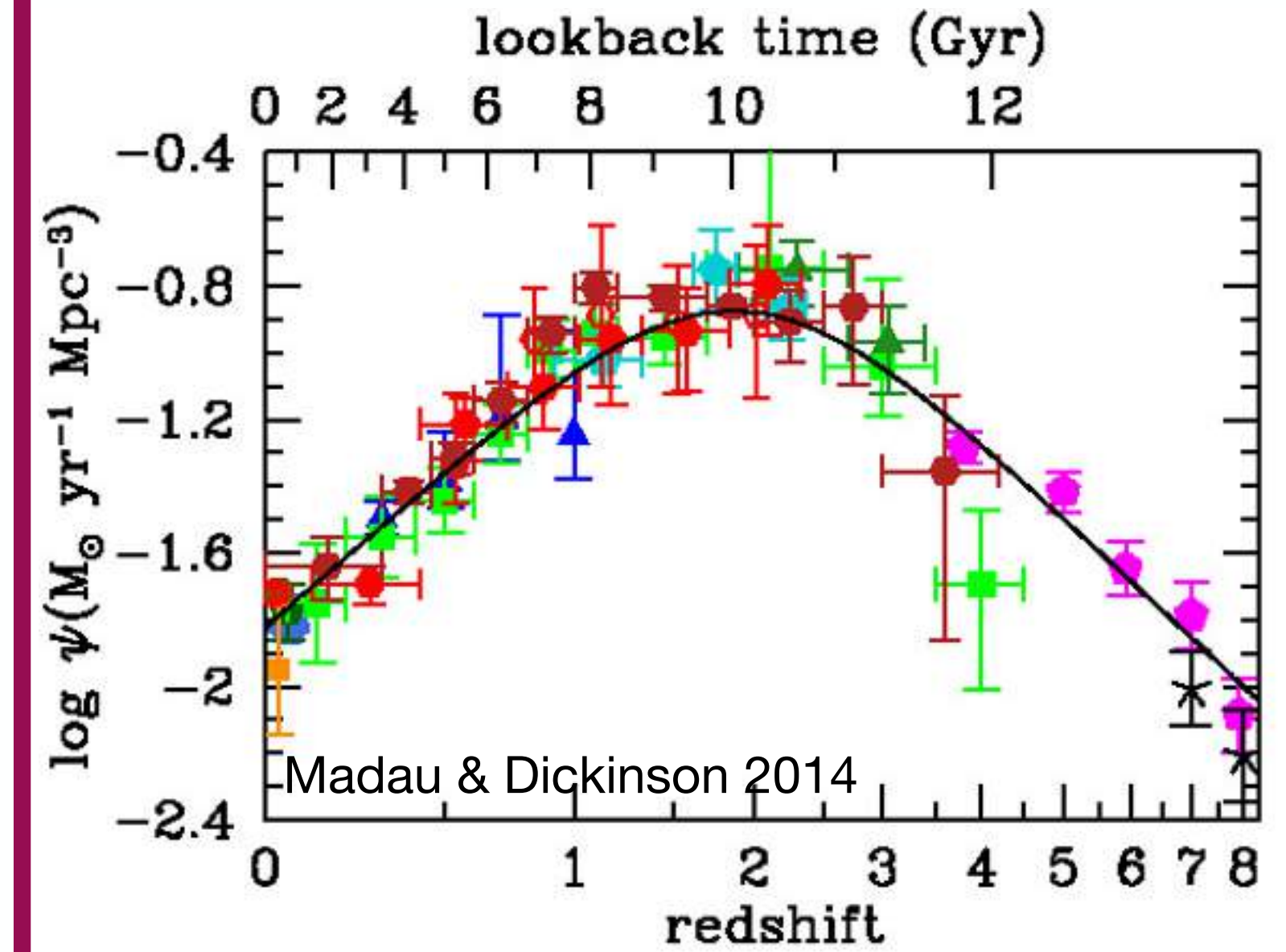
Testable implications/questions

Extinction properties/dust composition in different stellar environments



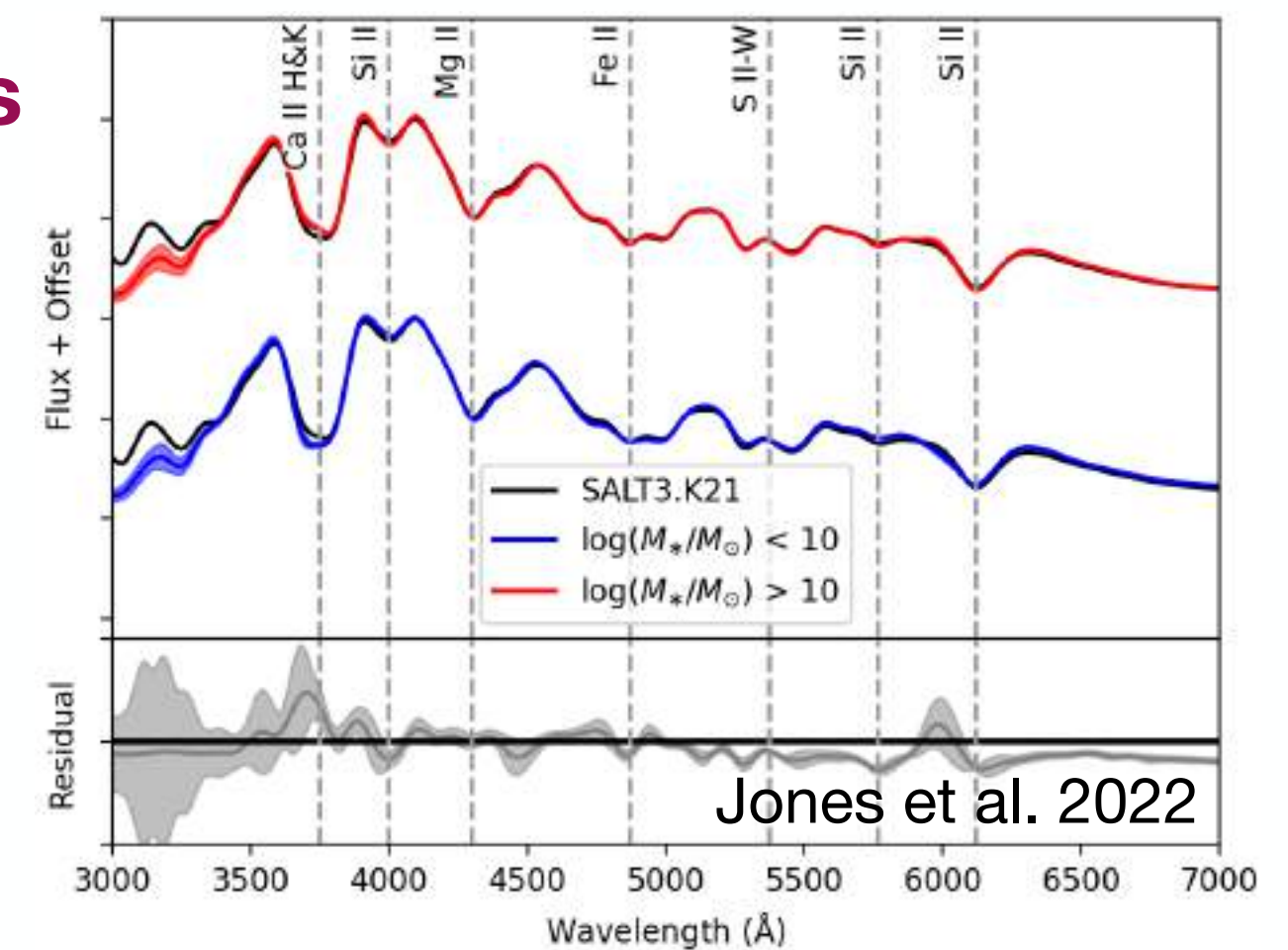
Salim et al. 2018

2-pops SN model



Relative fractions of SN populations should follow SFR

Spectroscopic differences between SN populations

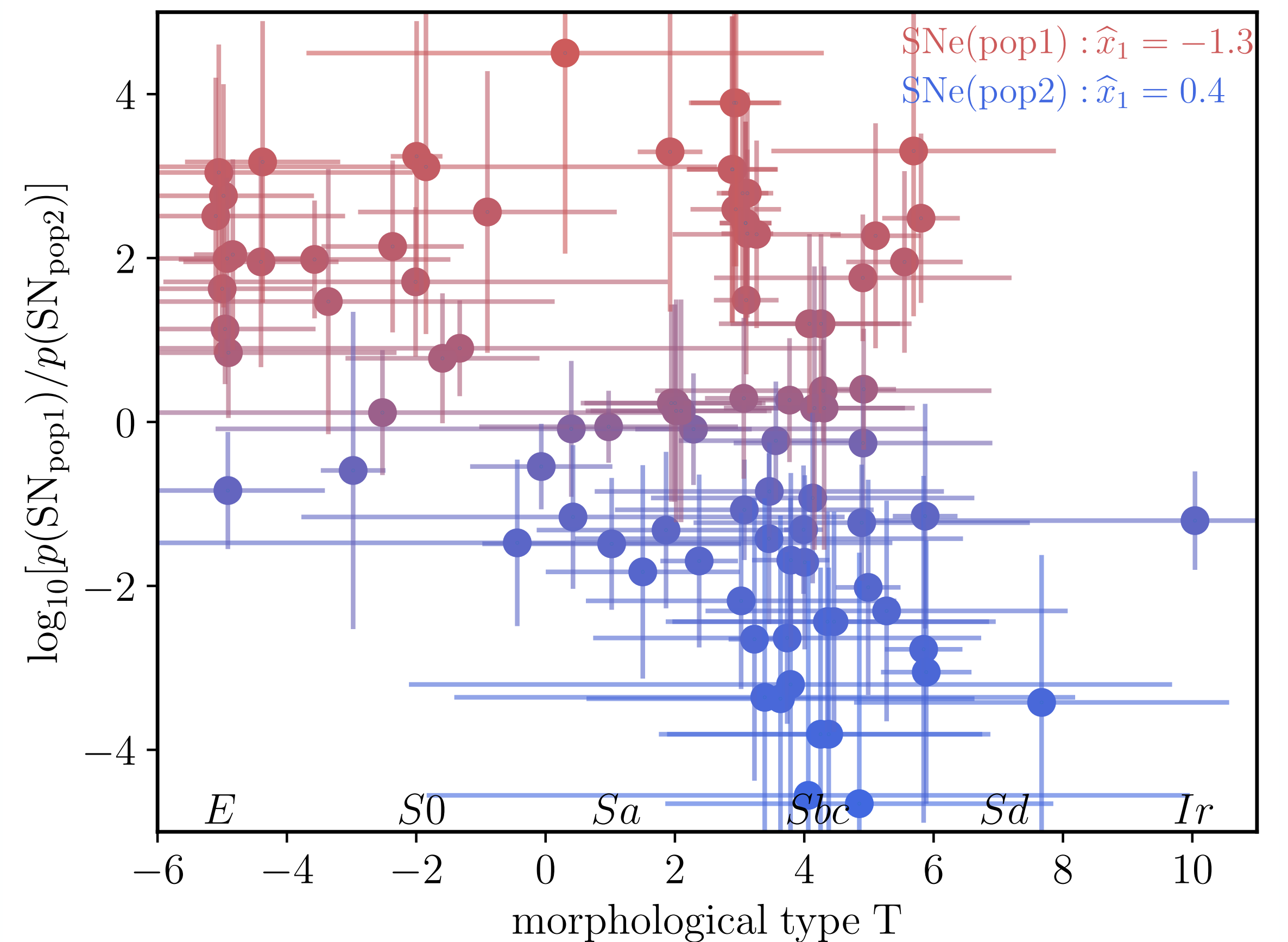
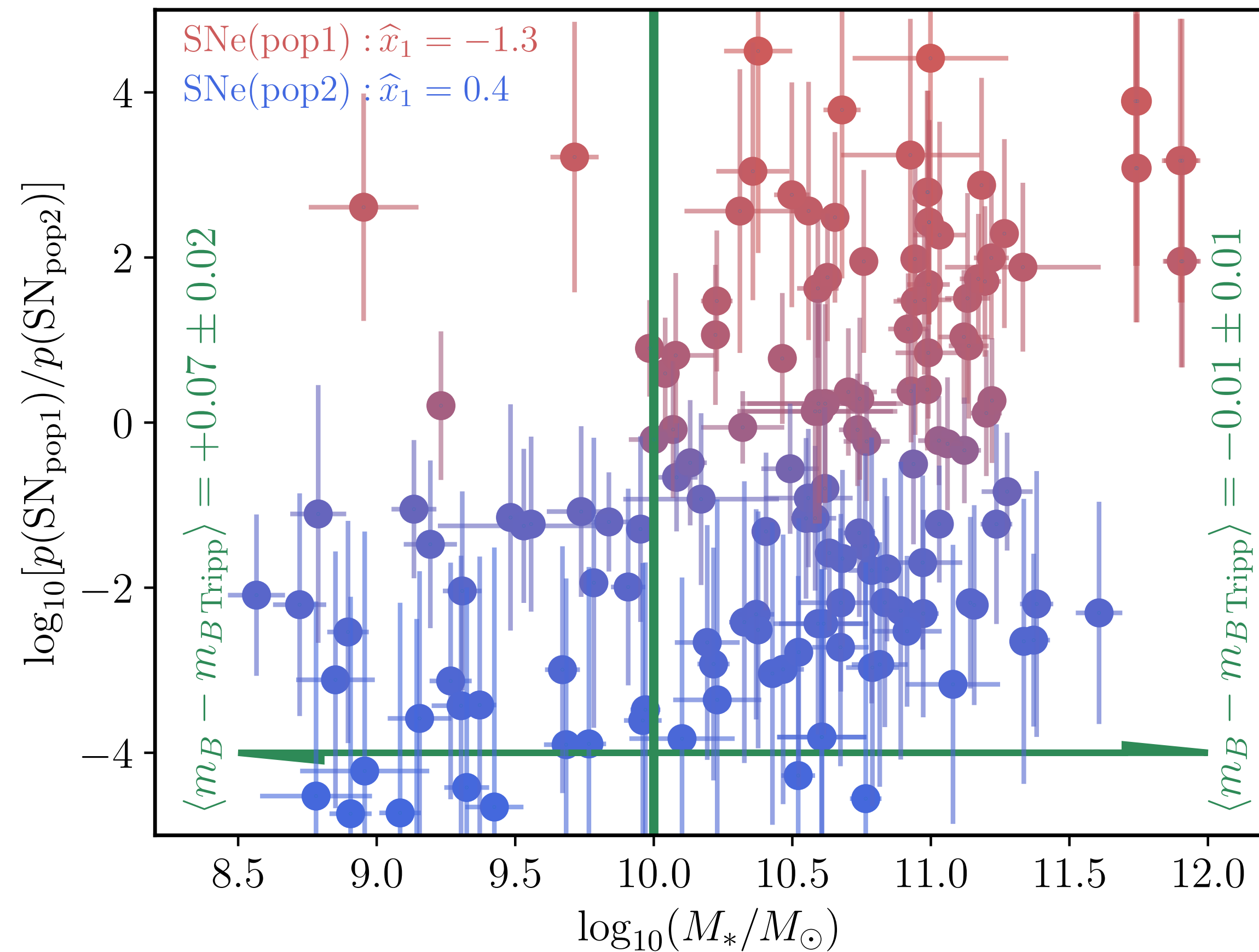


Hubble constant tension: SN physics vs EDE



“Step” correction is an emergent property

$$m_B = M_B - \alpha x_1 + \beta c + \gamma H(M_\star - M_0)$$



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$$m_B = M_B - \alpha x_1 + \beta c + \gamma H(M_\star - M_0)$$

